

Program Optimization Through Loop Vectorization

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Topics covered

- What are the microprocessor vector extensions or SIMD (Single Instruction Multiple Data Units)
- How to use them
 - Through the compiler via automatic vectorization
 - Manual transformations that enable vectorization
 - Directives to guide the compiler
 - Through intrinsics
- Main focus on vectorizing through the compiler.
 - Code more readable
 - Code portable



Outline

1. Intro
2. Data Dependences (Definition)
3. Overcoming limitations to SIMD-Vectorization
 - Data Dependences
 - Data Alignment
 - Aliasing
 - Non-unit strides
 - Conditional Statements
4. Vectorization with intrinsics



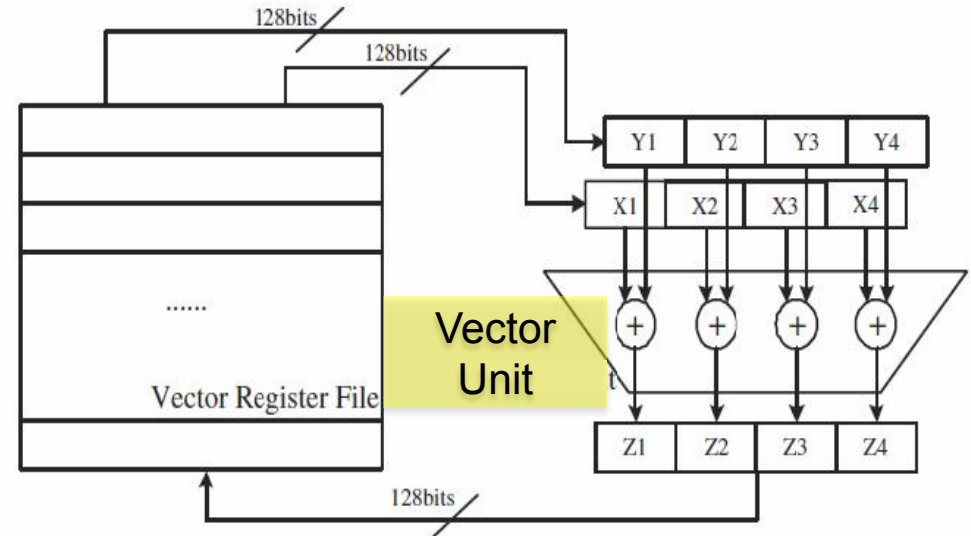
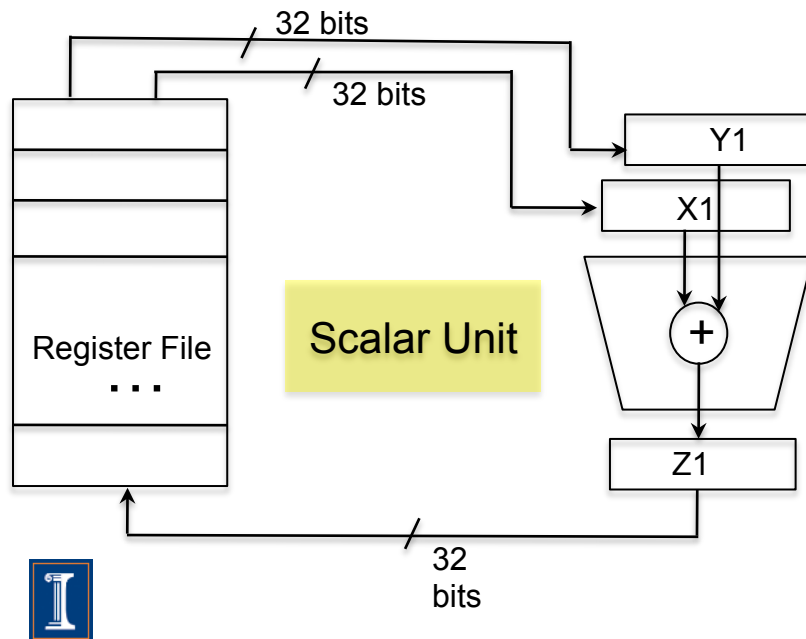
Simple Example

- Loop vectorization transforms a program so that the same operation is performed at the same time on several vector elements

n times
ld r1, addr1
ld r2, addr2
add r3, r1, r2
st r3, addr3

for (i=0; i<n; i++)
c[i] = a[i] + b[i];

$n/4$ times
ldv vr1, addr1
ldv vr2, addr2
addv vr3, vr1, vr2
stv vr3, addr3



SIMD Vectorization

- The use of SIMD units can speed up the program.
- Intel SSE and IBM AltiVec have 128-bit vector registers and functional units
 - 4 32-bit single precision floating point numbers
 - 2 64-bit double precision floating point numbers
 - 4 32-bit integer numbers
 - 2 64 bit integer
 - 8 16-bit integer or shorts
 - 16 8-bit bytes or chars
- Assuming a single ALU, these SIMD units can execute 4 single precision floating point number or 2 double precision operations in the time it takes to do only one of these operations by a scalar unit.



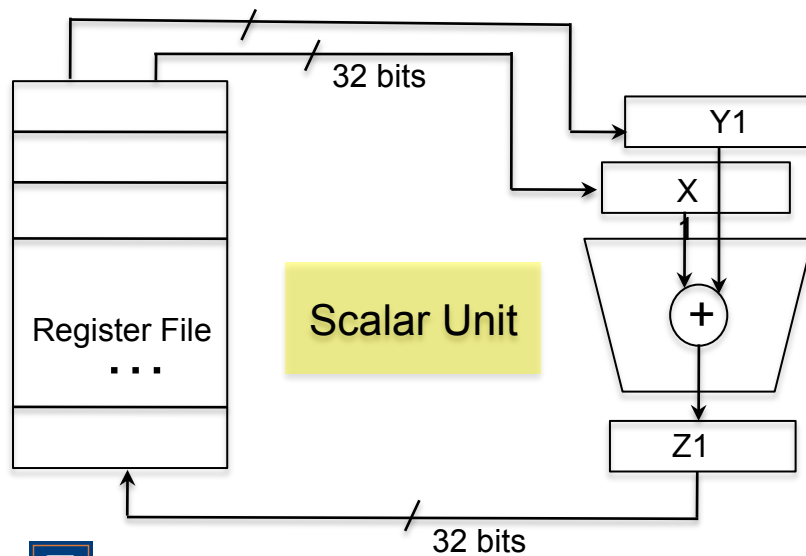
Executing Our Simple Example

S000

```
for (i=0; i<n; i++)  
  c[i] = a[i] + b[i];
```

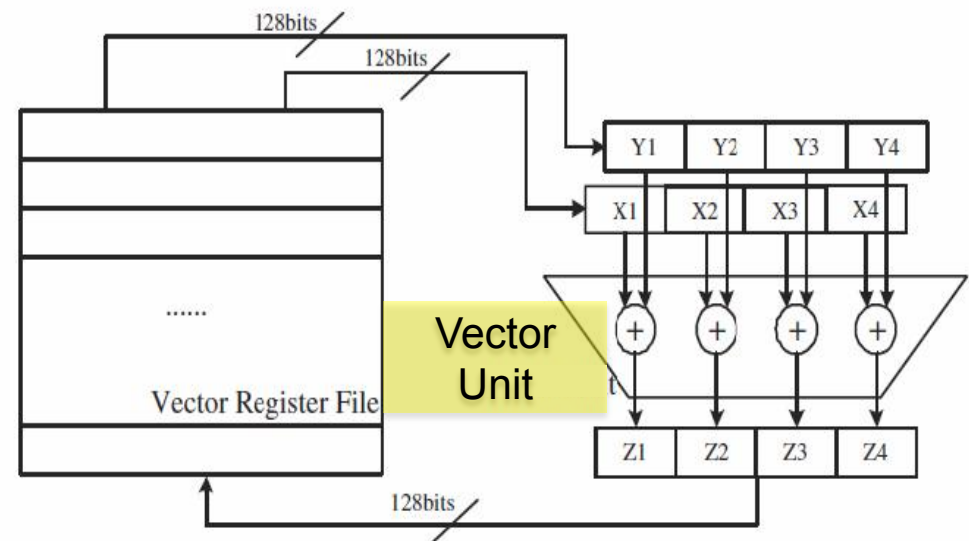
Intel Nehalem

Exec. Time scalar code: 6.1
Exec. Time vector code: 3.2
Speedup: 1.8



IBM Power 7

Exec. Time scalar code: 2.1
Exec. Time vector code: 1.0
Speedup: 2.1



How do we access the SIMD units?

- Three choices

1. C code and a vectorizing compiler

```
for (i=0; i<LEN; i++)  
    c[i] = a[i] + b[i];
```

2. Macros or Vector Intrinsics

```
void example(){  
    __m128 rA, rB, rC;  
    for (int i = 0; i < LEN; i+=4){  
        rA = _mm_load_ps(&a[i]);  
        rB = _mm_load_ps(&b[i]);  
        rC = _mm_add_ps(rA, rB);  
        _mm_store_ps(&c[i], rC);  
    }  
}
```

3. Assembly Language

```
..B8.5  
movaps    a(,%rdx,4), %xmm0  
addps     b(,%rdx,4), %xmm0  
movaps     %xmm0, c(,%rdx,4)  
addq      $4, %rdx  
cmpq      $rdi, %rdx  
jl        ..B8.5
```



Why should the compiler vectorize?

1. Easier
2. Portable across vendors and machines
 - Although compiler directives differ across compilers
3. Better performance of the compiler generated code
 - Compiler applies other transformations

Compilers make your codes (almost) machine independent

But, compilers fail:

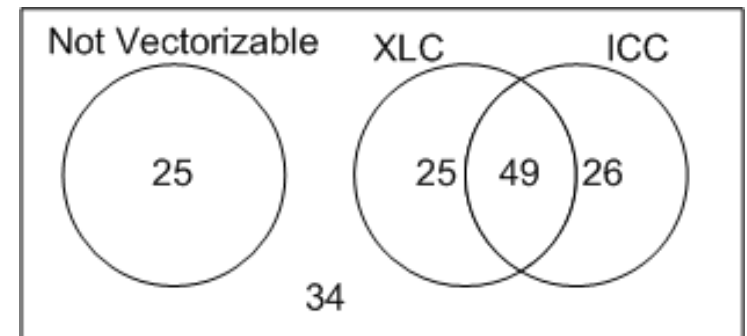
- Programmers need to provide the necessary information
- Programmers need to transform the code



How well do compilers vectorize?

Compiler	XLC	ICC	GCC
Loops			
Total	159		
Vectorized	74	75	32
Not vectorized	85	84	127
Average Speed Up	1.73	1.85	1.30

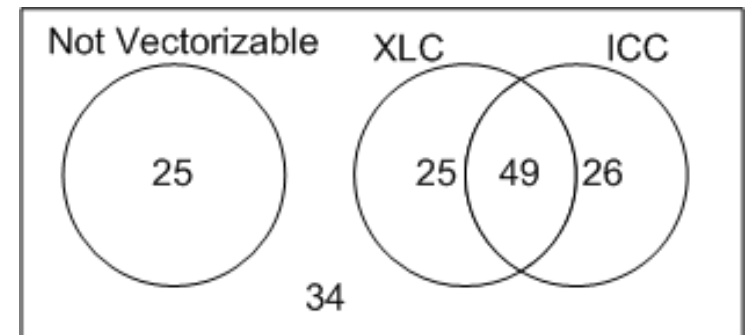
Compiler	XLC but not ICC	ICC but not XLC
Loops		
Vectorized	25	26



How well do compilers vectorize?

Compiler	XLC	ICC	GCC
Loops			
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Vectorized	74	75	32
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Compiler	XLC but not ICC	ICC but not XLC
Loops		
Vectorized	25	26



By adding manual vectorization the average speedup was 3.78 (versus 1.73 obtained by the XLC compiler)



How much programmer intervention?

- Next, three examples to illustrate what the programmer may need to do:
 - Add compiler directives
 - Transform the code
 - Program using vector intrinsics



Experimental results

- The tutorial shows results for two different platforms with their compilers:
 - Report generated by the compiler
 - Execution Time for each platform

Platform 1: Intel Nehalem
Intel Core i7 CPU 920@2.67GHz
Intel ICC compiler, version 11.1
OS Ubuntu Linux 9.04

Platform 2: IBM Power 7
IBM Power 7, 3.55 GHz
IBM xlc compiler, version 11.0
OS Red Hat Linux Enterprise 5.4

The examples use single precision floating point numbers



Compiler directives

```
void test(float* A,float* B,float* C,float* D, float* E)
{
    for (int i = 0; i <LEN; i++){
        A[i]=B[i]+C[i]+D[i]+E[i];
    }
}
```



Compiler directives

S1111

```
void test(float* A, float* B, float* C, float* D, float* E)
{
    for (int i = 0; i < LEN; i++){
        A[i]=B[i]+C[i]+D[i]+E[i];
    }
}
```

S1111

Intel Nehalem
Compiler report: Loop was not vectorized.
Exec. Time scalar code: 5.6
Exec. Time vector code: --
Speedup: --



S1111

```
void test(float* __restrict__ A,
float* __restrict__ B,
float* __restrict__ C,
float* __restrict__ D,
float* __restrict__ E)
{
    for (int i = 0; i < LEN; i++){
        A[i]=B[i]+C[i]+D[i]+E[i];
    }
}
```

S1111

Intel Nehalem
Compiler report: Loop was vectorized.
Exec. Time scalar code: 5.6
Exec. Time vector code: 2.2
Speedup: 2.5

Compiler directives

S1111

```
void test(float* A, float* B, float* C, float* D, float* E)
{
    for (int i = 0; i < LEN; i++){
        A[i]=B[i]+C[i]+D[i]+E[i];
    }
}
```

S1111

Power 7

Compiler report: Loop was not vectorized.

Exec. Time scalar code: 2.3

Exec. Time vector code: --

Speedup: --



S1111

```
void test(float* __restrict__ A,
float* __restrict__ B,
float* __restrict__ C,
float* __restrict__ D,
float* __restrict__ E)
{
    for (int i = 0; i < LEN; i++){
        A[i]=B[i]+C[i]+D[i]+E[i];
    }
}
```

S1111

Power 7

Compiler report: Loop was vectorized.

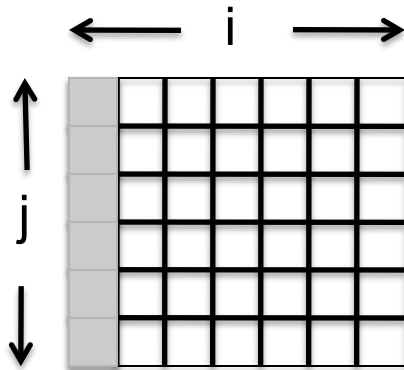
Exec. Time scalar code: 1.6

Exec. Time vector code: 0.6

Speedup: 2.7

Loop Transformations

```
for (int i=0;i<LEN;i++){  
    sum = (float) 0.0;  
    for (int j=0;j<LEN;j++){  
        sum += A[j][i];  
    }  
    B[i] = sum;  
}
```



```
for (int i=0;i<size;i++){  
    sum[i] = 0;  
    for (int j=0;j<size;j++){  
        sum[i] += A[j][i];  
    }  
    B[i] = sum[i];  
}
```



Loop Transformations

S136

```
for (int i=0;i<LEN;i++){  
    sum = (float) 0.0;  
    for (int j=0;j<LEN;j++){  
        sum += A[j][i];  
    }  
    B[i] = sum;  
}
```

S136_1

```
for (int i=0;i<LEN;i++){  
    sum[i] = (float) 0.0;  
    for (int j=0;j<LEN;j++){  
        sum[i] += A[j][i];  
    }  
    B[i]=sum[i];  
}
```

S136_2

```
for (int i=0;i<LEN;i++){  
    B[i] = (float) 0.0;  
    for (int j=0;j<LEN;j++){  
        B[i] += A[j][i];  
    }  
}
```

S136

Intel Nehalem
Compiler report: Loop was not vectorized. Vectorization possible but seems inefficient
Exec. Time scalar code: 3.7
Exec. Time vector code: --
Speedup: --

S136_1

Intel Nehalem
report: Permuted loop was vectorized.
scalar code: 1.6
vector code: 0.6
Speedup: 2.6

S136_2

Intel Nehalem
report: Permuted loop was vectorized.
scalar code: 1.6
vector code: 0.6
Speedup: 2.6



Loop Transformations

S136

```
for (int i=0;i<LEN;i++){
  sum = (float) 0.0;
  for (int j=0;j<LEN;j++){
    sum += A[j][i];
  }
  B[i] = sum;
}
```

S136_1

```
for (int i=0;i<LEN;i++){
  sum[i] = (float) 0.0;
  for (int j=0;j<LEN;j++){
    sum[i] += A[j][i];
  }
  B[i]=sum[i];
}
```

S136_2

```
for (int i=0;i<LEN;i++){
  B[i] = (float) 0.0;
  for (int j=0;j<LEN;j++){
    B[i] += A[j][i];
  }
}
```

S136

IBM Power 7

Compiler report: Loop was not SIMD vectorized

Exec. Time scalar code: 2.0

Exec. Time vector code: --

Speedup: --

S136_1

IBM Power 7

report: Loop interchanging applied.
Loop was SIMD vectorized

scalar code: 0.4

vector code: 0.2

Speedup: 2.0

S136_2

IBM Power 7

report: Loop interchanging applied.
Loop was SIMD

scalar code: 0.4

vector code: 0.16

Speedup: 2.7



Intrinsics (SSE)

```
#define n 1024
__attribute__((aligned(16))) float a[n], b[n], c[n];
int main() {
    for (i = 0; i < n; i++) {
        c[i]=a[i]*b[i];
    }
}
```



```
#include <xmmintrin.h>
#define n 1024
__attribute__((aligned(16))) float a[n], b[n], c[n];

int main() {
    __m128 rA, rB, rC;
    for (i = 0; i < n; i+=4) {
        rA = _mm_load_ps(&a[i]);
        rB = _mm_load_ps(&b[i]);
        rC= _mm_mul_ps(rA,rB);
        _mm_store_ps(&c[i], rC);
    }
}
```



Intrinsics (Altivec)

```
#define n 1024
__attribute__((aligned(16))) float a[n],b[n],c[n];
...
for (int i=0; i<LEN; i++)
    c[i]=a[i]*b[i];
```



```
vector float rA,rB,rC,r0;           // Declares vector registers
r0 = vec_xor(r0,r0);                 // Sets r0 to {0,0,0,0}
for (int i=0; i<LEN; i+=4){          // Loop stride is 4
    rA = vec_ld(0, &a[i]);           // Load values to rA
    rB = vec_ld(0, &b[i]);           // Load values to rB
    rC = vec_madd(rA,rB,r0);          // rA and rB are multiplied
    vec_st(rC, 0, &c[i]);            // rC is stored to the c[i:i+3]
}
```



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 - Aliasing
 - Non-unit strides
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Data dependences

- The notion of dependence is the foundation of the process of vectorization.
- It is used to build a calculus of program transformations that can be applied manually by the programmer or automatically by a compiler.



Definition of Dependence

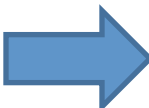
- A statement S is said to be data dependent on statement T if
 - T executes before S in the original sequential/scalar program
 - S and T access the same data item
 - At least one of the accesses is a write.



Data dependences and vectorization

- Loop dependences guide vectorization
- **Main idea:** A statement inside a loop which is not in a cycle of the dependence graph can be vectorized.

```
for (i=0; i<n; i++){  
S1  a[i] = b[i] + 1;  
}
```



```
a[0:n-1] = b[0:n-1] + 1;
```

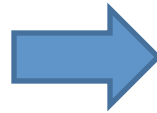
S1



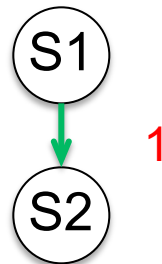
Data dependences and vectorization

- **Main idea:** A statement inside a loop which is not in a cycle of the dependence graph can be vectorized.

```
for (i=1; i<n; i++){  
S1  a[i] = b[i] + 1;  
S2  c[i] = a[i-1] + 2;  
}
```



```
a[1:n] = b[1:n] + 1;  
c[1:n] = a[0:n-1] + 2;
```



Data dependences and transformations

- When cycles are present, vectorization can be achieved by:
 - Separating (distributing) the statements not in a cycle
 - Removing dependences
 - Freezing loops
 - Changing the algorithm

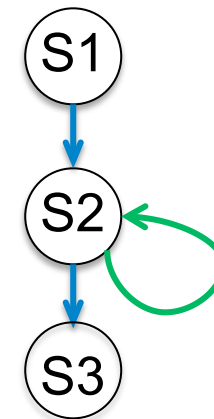


Distributing

```
for (i=1; i<n; i++){  
S1  b[i] = b[i] + c[i];  
S2  a[i] = a[i-1]*a[i-2]+b[i];  
S3  c[i] = a[i] + 1;  
}
```



```
b[1:n-1] = b[1:n-1] + c[1:n-1];  
for (i=1; i<n; i++){  
    a[i] = a[i-1]*a[i-2]+b[i];  
}  
c[1:n-1] = a[1:n-1] + 1;
```



Removing dependencies

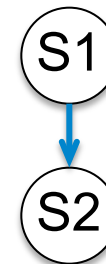
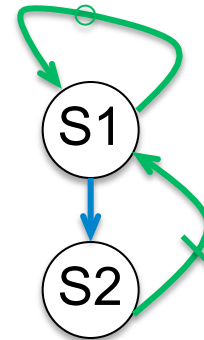
```
for (i=0; i<n; i++){  
S1   a = b[i] + 1;  
S2   c[i] = a + 2;  
}
```



```
for (i=0; i<n; i++){  
S1   a'[i] = b[i] + 1;  
S2   c[i] = a'[i] + 2;  
}  
a=a'[n-1]
```

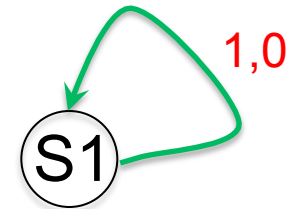


```
S1   a'[0:n-1] = b[0:n-1] + 1;  
S2   c[0:n-1] = a'[0:n-1] + 2;  
a=a'[n-1]
```



Freezing Loops

```
for (i=1; i<n; i++) {  
    for (j=1; j<n; j++) {  
        a[i][j]=a[i][j]+a[i-1][j];  
    }  
}
```



Ignoring (freezing) the outer loop:

```
for (j=1; j<n; j++) {  
    a[i][j]=a[i][j]+a[i-1][j];  
}
```



```
for (i=1; i<n; i++) {  
    a[i][1:n-1]=a[i][1:n-1]+a[i-1][1:n-1];  
}
```



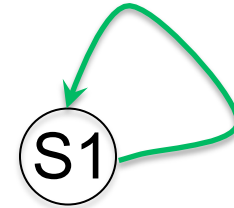
Changing the algorithm

- When there is a recurrence, it is necessary to change the algorithm in order to vectorize.
- Compiler use pattern matching to identify the recurrence and then replace it with a parallel version.
- Examples of recurrences include:
 - Reductions ($S += A[i]$)
 - Linear recurrences ($A[i] = B[i] * A[i-1] + C[i]$)
 - Boolean recurrences ($\text{if } (A[i] > \text{max}) \text{ max} = A[i]$)



Changing the algorithm (cont.)

▪
S1 a[0]=b[0];
for (i=1; i<n; i++)
S2 a[i]=a[i-1]+b[i];

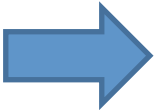


a[0:n-1]=b[0:n-1];
for (i=0;i<k;i++) /* n = 2^k */
a[2**i:n-1]=a[2**i:n-1]+b[0:n-2**i];



Stripmining

- Stripmining is a simple transformation.

```
for (i=1; i<n; i++){  
    ...  
}  
      
/* n is a multiple of q */  
for (k=1; k<n; k+=q){  
    for (i=k; i<k+q-1; i++){  
        ...  
    }  
}
```

- It is typically used to improve locality.



Stripmining (cont.)

- Stripmining is often used when vectorizing

```
for (i=1; i<n; i++){  
    a[i] = b[i] + 1;  
    c[i] = a[i] + 2;  
}
```



stripmine

```
for (k=1; k<n; k+=q){  
    /* q could be size of vector register */  
    for (i=k; i < k+q; i++){  
        a[i] = b[i] + 1;  
        c[i] = a[i-1] + 2;  
    }  
}
```



vectorize

```
for (i=1; i<n; i+=q){  
    a[i:i+q-1] = b[i:i+q-1] + 1;  
    c[i:i+q-1] = a[i:i+q] + 2;  
}
```



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Loop Vectorization

- Loop Vectorization is not always a legal and profitable transformation.
- Compiler needs:
 - Compute the dependences
 - The compiler figures out dependences by
 - Solving a system of (integer) equations (with constraints)
 - Demonstrating that there is no solution to the system of equations
 - Remove cycles in the dependence graph
 - Determine data alignment
 - Vectorization is profitable



Simple Example

- Loop vectorization transforms a program so that the same operation is performed at the same time on several of the elements of the vectors

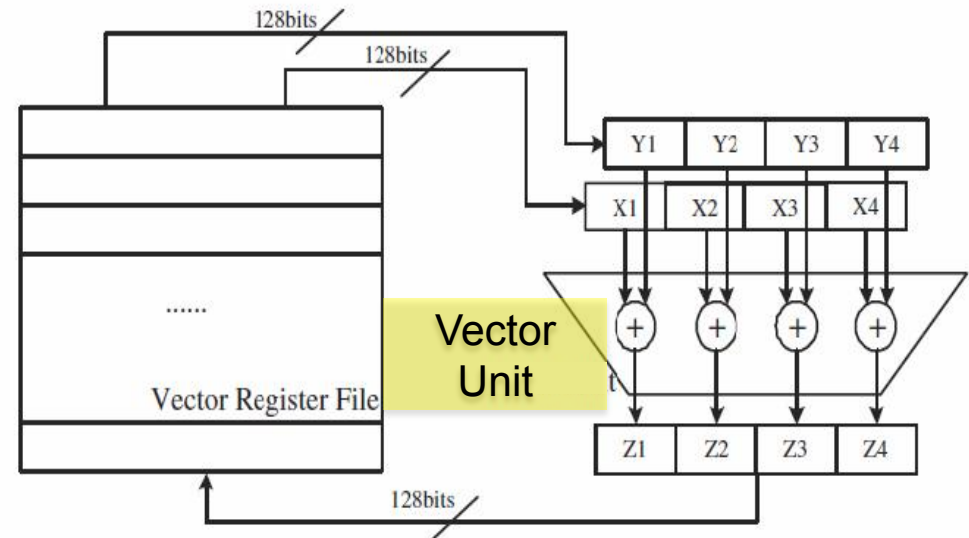
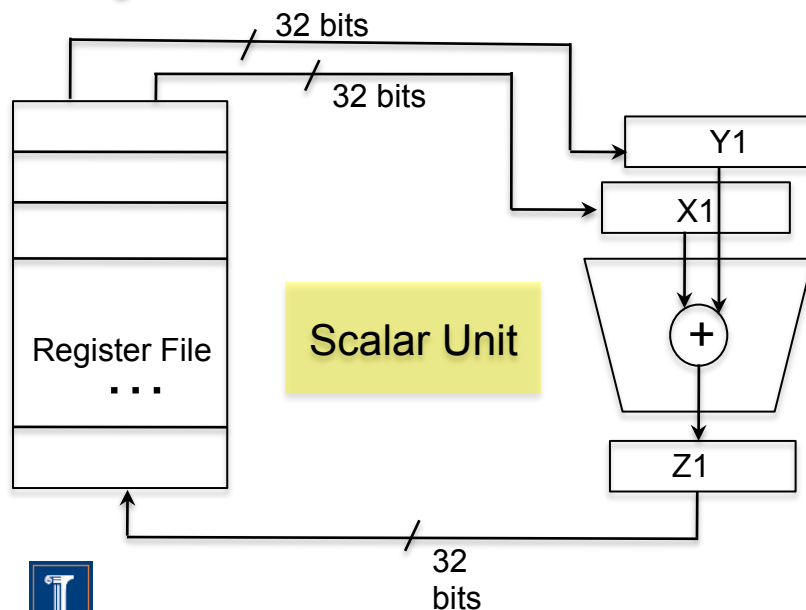
n times

```
ld r1, addr1
ld r2, addr2
add r3, r1, r2
st r3, addr3
```

```
for (i=0; i<LEN; i++)
    c[i] = a[i] + b[i];
```

$n/4$ times

```
ldv vr1, addr1
ldv vr2, addr2
addv vr3, vr1, vr2
stv vr3m addr3
```



Loop Vectorization

- When vectorizing a loop with several statements the compiler need to strip-mine the loop and then apply loop distribution

```
for (i=0; i<LEN; i++){  
S1 a[i]=b[i]+(float)1.0;  
S2 c[i]=b[i]+(float)2.0;  
}  
→  
for (i=0; i<LEN; i+=strip_size){  
  for (j=i; j<i+strip_size; j++)  
    a[j]=b[j]+(float)1.0;  
  for (j=i; j<i+strip_size; j++)  
    c[j]=b[j]+(float)2.0;  
}
```

i=0 i=1 i=2 i=3 i=4 i=5 i=6 i=7

(S1) (S1) (S1) (S1) (S1) (S1) (S1) (S1)

(S2) (S2) (S2) (S2) (S2) (S2) (S2) (S2)



Loop Vectorization

- When vectorizing a loop with several statements the compiler need to strip-mine the loop and then apply loop distribution

```
for (i=0; i<LEN; i++){  
S1 a[i]=b[i]+(float)1.0;  
S2 c[i]=b[i]+(float)2.0;  
}  
→  
for (i=0; i<LEN; i+=strip_size){  
  for (j=i; j<i+strip_size; j++)  
    a[j]=b[j]+(float)1.0;  
  for (j=i; j<i+strip_size; j++)  
    c[j]=b[j]+(float)2.0;  
}
```

i=0 i=1 i=2 i=3 i=4 i=5 i=6 i=7



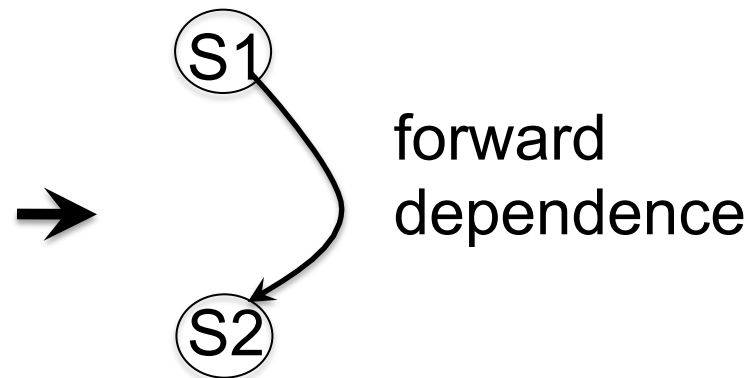
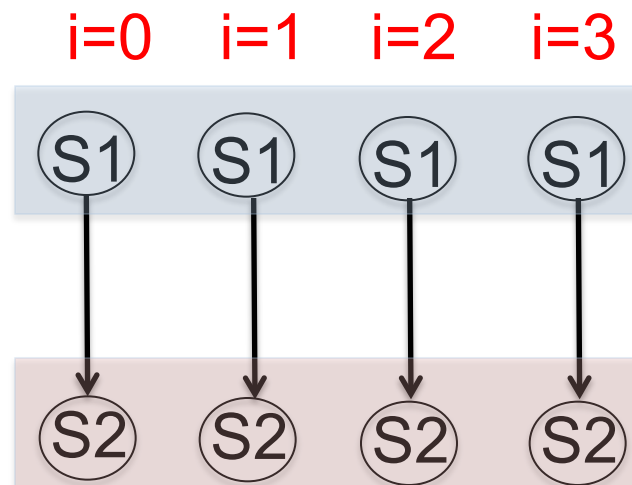
Dependence Graphs and Compiler Vectorization

- No dependences: previous two slides
- Acyclic graphs:
 - All dependences are forward:
 - Vectorized by the compiler
 - Some backward dependences:
 - Sometimes vectorized by the compiler
- Cycles in the dependence graph
 - Self-antidependence:
 - Vectorized by the compiler
 - Recurrence:
 - Usually not vectorized by the the compiler
 - Other examples



Acyclic Dependence Graphs: Forward Dependences

```
for (i=0; i<LEN; i++) {  
S1 a[i]= b[i] + c[i]  
S2 d[i] = a[i] + (float) 1.0;  
}
```



Acyclic Dependence Graphs: Forward Dependences

S113

```
for (i=0; i<LEN; i++) {  
    a[i]= b[i] + c[i]  
    d[i] = a[i] + (float) 1.0;  
}
```

Intel Nehalem

Compiler report: Loop was
vectorized

Exec. Time scalar code: 10.2

Exec. Time vector code: 6.3

Speedup: 1.6

IBM Power 7

Compiler report: Loop was SIMD
vectorized

Exec. Time scalar code: 3.1

Exec. Time vector code: 1.5

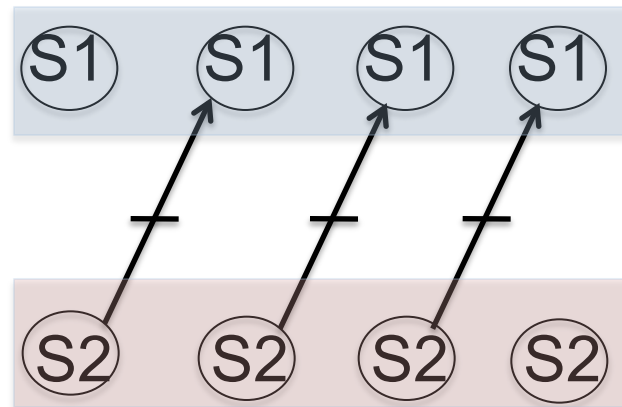
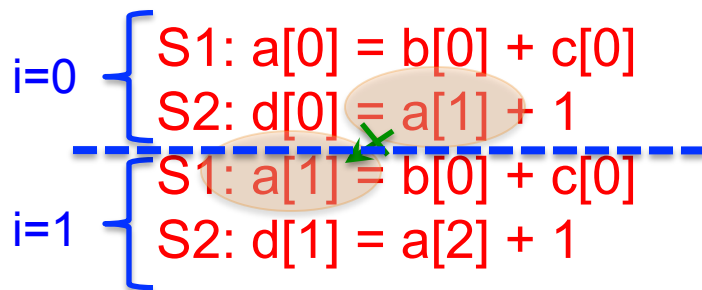
Speedup: 2.0



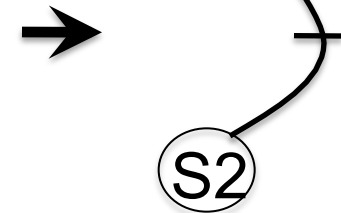
Acyclic Dependenden Graphs

Backward Dependences (I)

```
for (i=0; i<LEN; i++) {  
S1  a[i]= b[i] + c[i]  
S2  d[i] = a[i+1] + (float) 1.0;  
}
```



backward
dependence



This loop cannot be vectorized as it is

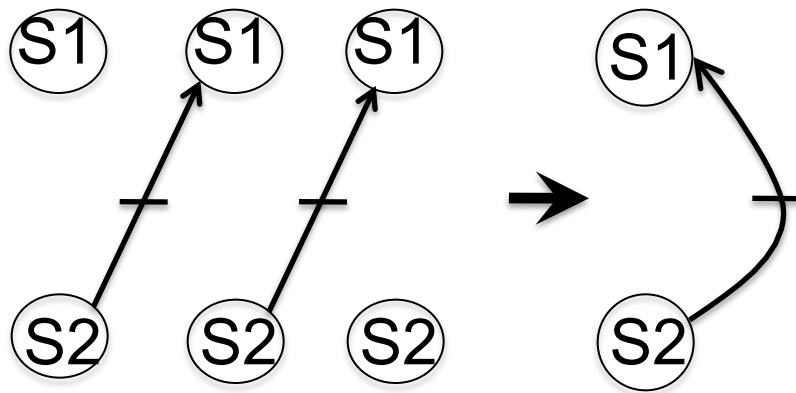


Acyclic Dependenden Graphs

Backward Dependences (I)

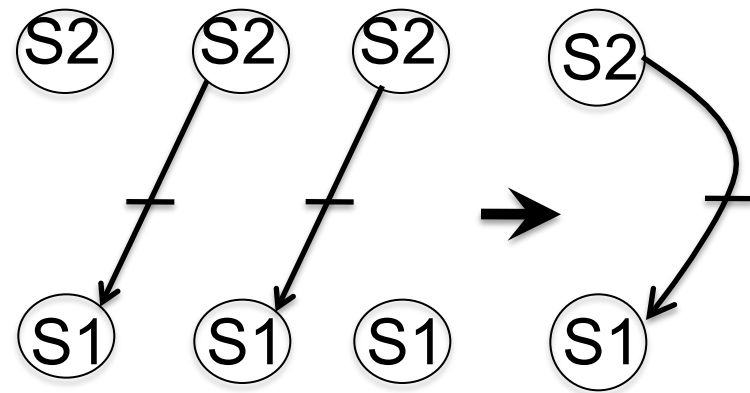
Reorder of statements

```
for (i=0; i<LEN; i++) {
S1  a[i]= b[i] + c[i]
S2  d[i] = a[i+1] + (float) 1.0;
}
```



backward
depedence

```
for (i=0; i<LEN; i++) {
S2  d[i] = a[i+1]+(float)1.0;
S1  a[i]= b[i] + c[i];
}
```



forward
depedence



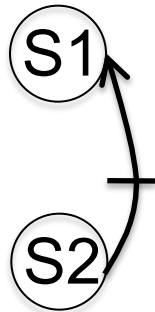
Acyclic Dependenden Graphs

Backward Dependences (I)

S114

```
for (i=0; i<LEN; i++) {  
    a[i]= b[i] + c[i];  
    d[i] = a[i+1]+(float)1.0;  
}
```

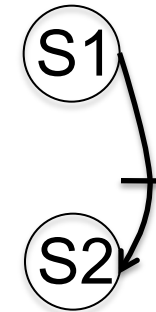
S114



S114_1

```
for (i=0; i<LEN; i++) {  
    d[i] = a[i+1]+(float)1.0;  
    a[i]= b[i] + c[i];  
}
```

S114_1



Intel Nehalem

Compiler report: Loop was not vectorized. Existence of vector dependence

Exec. Time scalar code: 12.6

Exec. Time vector code: --

Speedup: --

Intel Nehalem

Compiler report: Loop was vectorized

Exec. Time scalar code: 10.7

Exec. Time vector code: 9.4

Speedup: 1.03

Speedup vs non-reordered code: 1.35



Acyclic Dependenden Graphs

Backward Dependences (I)

S114

```
for (i=0; i<LEN; i++) {  
    a[i]= b[i] + c[i];  
    d[i] = a[i+1]+(float)1.0;  
}
```

S114_1

```
for (i=0; i<LEN; i++) {  
    d[i] = a[i+1]+(float)1.0;  
    a[i]= b[i] + c[i];  
}
```

The IBM XLC compiler generated the same code in both cases

S114

IBM Power 7

Compiler report: Loop was SIMD
vectorized

Exec. Time scalar code: 1.2

Exec. Time vector code: 0.6

Speedup: 2.0

S114_1

IBM Power 7

Compiler report: Loop was SIMD
vectorized

Exec. Time scalar code: 1.2

Exec. Time vector code: 0.6

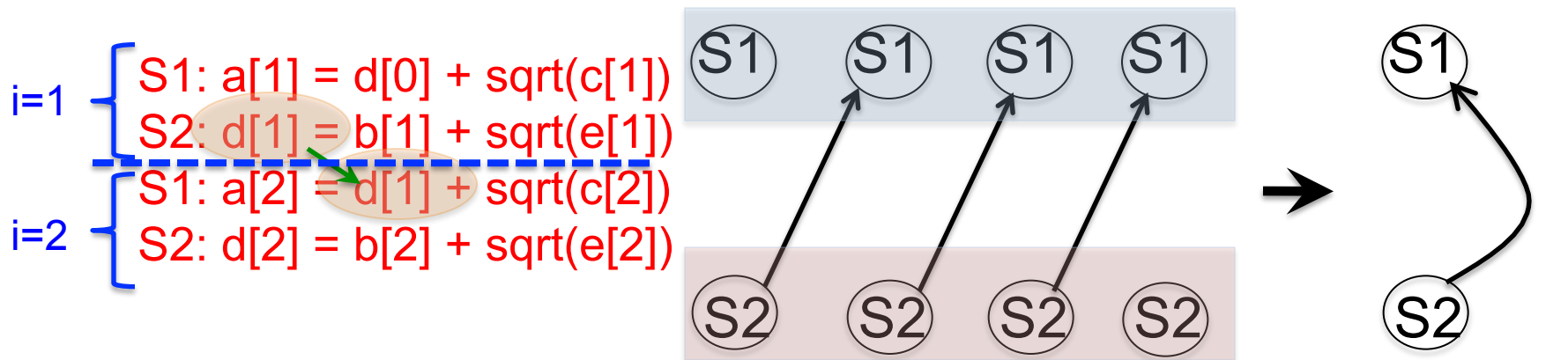
Speedup: 2.0



Acyclic Dependenden Graphs

Backward Dependences (II)

```
for (int i = 1; i < LEN; i++) {  
S1 a[i] = d[i-1] + (float)sqrt(c[i]);  
S2 d[i] = b[i] + (float)sqrt(e[i]);  
}
```



This loop cannot be vectorized as it is

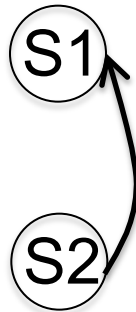


Acyclic Dependenden Graphs

Backward Dependences (II)

S214

```
for (int i=1;i<LEN;i++) {  
    a[i]=d[i-1]+(float)sqrt(c[i]);  
    d[i]=b[i]+(float)sqrt(e[i]);  
}
```



S114

S214_1

```
for (int i=1;i<LEN;i++) {  
    d[i]=b[i]+(float)sqrt(e[i]);  
    a[i]=d[i-1]+(float)sqrt(c[i]);  
}
```



S114_1

Intel Nehalem

Compiler report: Loop was not vectorized. Existence of vector dependence

Exec. Time scalar code: 7.6

Exec. Time vector code: --

Speedup: --

Intel Nehalem

Compiler report: Loop was vectorized

Exec. Time scalar code: 7.6

Exec. Time vector code: 3.8

Speedup: 2.0



Acyclic Dependenden Graphs

Backward Dependences (II)

S114

```
for (i=0; i<LEN; i++) {  
    a[i]= b[i] + c[i];  
    d[i] = a[i+1]+(float)1.0;  
}
```

S114_1

```
for (i=0; i<LEN; i++) {  
    d[i] = a[i+1]+(float)1.0;  
    a[i]= b[i] + c[i];  
}
```

The IBM XLC compiler generated the same code in both cases

S114

IBM Power 7

Compiler report: Loop was SIMD
vectorized

Exec. Time scalar code: 3.3

Exec. Time vector code: 1.8

Speedup: 1.8

S114_1

IBM Power 7

Compiler report: Loop was SIMD
vectorized

Exec. Time scalar code: 3.3

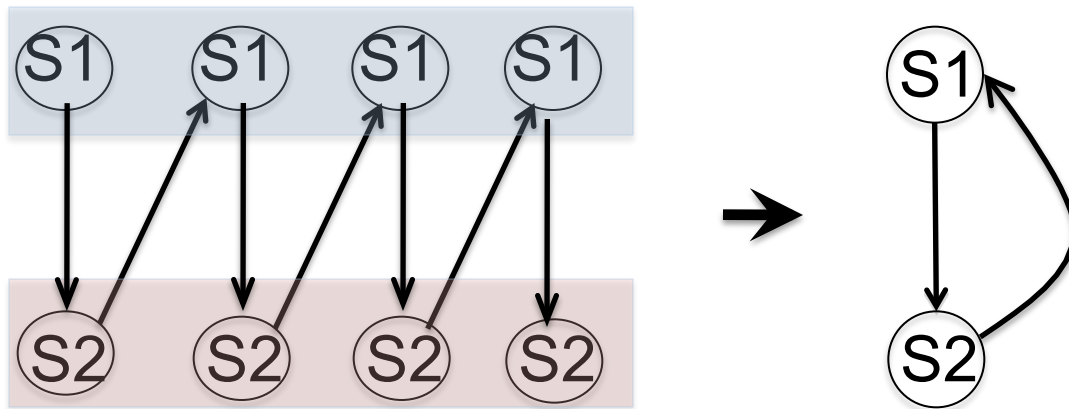
Exec. Time vector code: 1.8

Speedup: 1.8



Cycles in the DG (I)

```
for (int i=0;i<LEN-1;i++){  
  S1  b[i]    = a[i] + (float) 1.0;  
  S2  a[i+1] = b[i] + (float) 2.0;  
}
```



This loop cannot be vectorized (as it is)
Statements cannot be simply reordered



Cycles in the DG (I)

S115

```
for (int i=0;i<LEN-1;i++){  
    b[i]    = a[i] + (float) 1.0;  
    a[i+1] = b[i] + (float) 2.0;  
}
```

S115

Intel Nehalem

Compiler report: Loop was not vectorized.

Existence of vector dependence

Exec. Time scalar code: 12.1

Exec. Time vector code: --

Speedup: --



Cycles in the DG (I)

S115

```
for (int i=0;i<LEN-1;i++){  
    b[i]    = a[i] + (float) 1.0;  
    a[i+1] = b[i] + (float) 2.0;  
}
```

S115

IBM Power 7

Compiler report: Loop was SIMD vectorized

Exec. Time scalar code: 3.1

Exec. Time vector code: 2.2

Speedup: 1.4



Cycles in the DG (I)

S115

```
for (int i=0;i<LEN-1;i++){  
    b[i]    = a[i] + (float) 1.0;  
    a[i+1] = b[i] + (float) 2.0;  
}
```

The IBM XLC compiler applies
forward substitution and reordering
to vectorize the code

compiler generated code

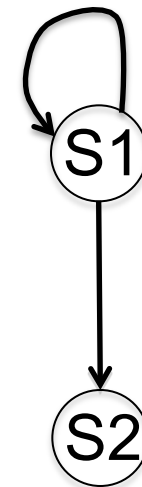
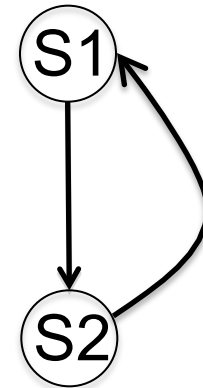
This loop is
not vectorized

```
for (int i=0;i<LEN-1;i++){  
    a[i+1]=a[i]+(float)1.0+(float)2.0;
```

b[i]

This loop is
vectorized

```
for (int i=0;i<LEN-1;i++){  
    b[i]    = a[i] + (float) 1.0;
```



Cycles in the DG (I)

S115

```
for (int i=0;i<LEN-1;i++){  
    b[i]  =a[i]+(float)1.0;  
    a[i+1]=b[i]+(float)2.0;  
}
```

S215

```
for (int i=0;i<LEN-1;i++){  
    b[i]=a[i]+d[i]*d[i]+c[i]*c[i]+c[i]*d[i];  
    a[i+1]=b[i]+(float)2.0;  
}
```

Will the IBM XLC compiler
vectorize this code as before?



Cycles in the DG (I)

S115

```
for (int i=0;i<LEN-1;i++){  
    b[i]  =a[i]+(float)1.0;  
    a[i+1]=b[i]+(float)2.0;  
}
```

S215

```
for (int i=0;i<LEN-1;i++){  
    b[i]=a[i]+d[i]*d[i]+c[i]*c[i]+c[i]*d[i];  
    a[i+1]=b[i]+(float)2.0;  
}
```

Will the IBM XLC compiler
vectorize this code as before?

To vectorize, the compiler needs to do this

```
for (int i=0;i<LEN-1;i++)  
    a[i+1]=a[i]+d[i]*d[i]+c[i]*c[i]+c[i]*d[i]+(float)2.0;  
  
for (int i=0;i<LEN-1;i++)  
    b[i]=a[i]+d[i]*d[i]+c[i]*c[i]+c[i]*d[i]+(float) 1.0;
```



Cycles in the DG (I)

S115

```
for (int i=0;i<LEN-1;i++){  
    b[i]  =a[i]+(float)1.0;  
    a[i+1]=b[i]+(float)2.0;  
}
```

S215

```
for (int i=0;i<LEN-1;i++){  
    b[i]=a[i]+d[i]*d[i]+c[i]*c[i]+c[i]*d[i];  
    a[i+1]=b[i]+(float)2.0;  
}
```

Will the IBM XLC compiler
vectorize this code as before?

No, the compiler does not
vectorize S215 because
it is not cost-effective

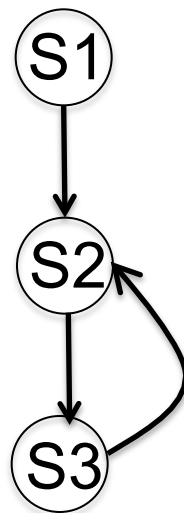
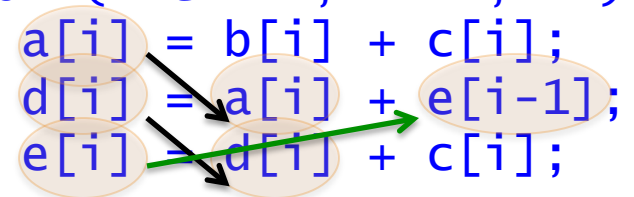
```
for (int i=0;i<LEN-1;i++)  
    a[i+1]=a[i]+d[i]*d[i]+c[i]*c[i]+c[i]*d[i]+(float)2.0;  
  
for (int i=0;i<LEN-1;i++)  
    b[i]=a[i]+d[i]*d[i]+c[i]*c[i]+c[i]*d[i]+(float) 1.0;
```



Cycles in the DG (II)

A loop can be partially vectorized

```
for (int i=1;i<LEN;i++){  
S1  a[i] = b[i] + c[i];  
S2  d[i] = a[i] + e[i-1];  
S3  e[i] = d[i] + c[i];  
}
```



S1 can be vectorized
S2 and S3 cannot be vectorized (as they are)



Cycles in the DG (II)

S116

```
for (int i=1;i<LEN;i++){  
    a[i] = b[i] + c[i];  
    d[i] = a[i] + e[i-1];  
    e[i] = d[i] + c[i];  
}
```

S116

```
for (int i=1;i<LEN;i++){  
    a[i] = b[i] + c[i];  
    d[i] = a[i] + e[i-1];  
    e[i] = d[i] + c[i];  
}
```

S116

Intel Nehalem

Compiler report: Loop was partially vectorized

Exec. Time scalar code: 14.7

Exec. Time vector code: 18.1

Speedup: 0.8

S116

IBM Power 7

Compiler report: Loop was not SIMD vectorized because a data dependence prevents SIMD vectorization

Exec. Time scalar code: 13.5

Exec. Time vector code: --

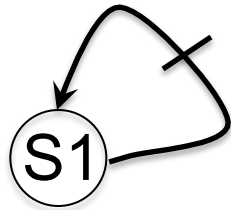
Speedup: --



Cycles in the DG (III)

```
for (int i=0;i<LEN-1;i++){  
S1  a[i]=a[i+1]+b[i];  
}
```

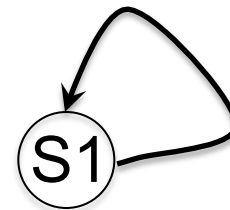
$a[0]=a[1]+b[0]$
 $a[1]=a[2]+b[1]$
 $a[2]=a[3]+b[2]$
 $a[3]=a[4]+b[3]$



Self-antidependence
can be vectorized

```
for (int i=1;i<LEN;i++){  
S1  a[i]=a[i-1]+b[i];  
}
```

$a[1]=a[0]+b[1]$
 $a[2]=a[1]+b[2]$
 $a[3]=a[2]+b[3]$
 $a[4]=a[3]+b[4]$



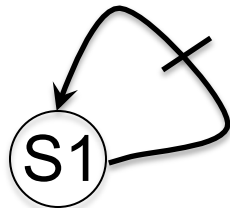
Self true-dependence
can not vectorized
(as it is)



Cycles in the DG (III)

S117

```
for (int i=0;i<LEN-1;i++){  
S1  a[i]=a[i+1]+b[i];  
}
```

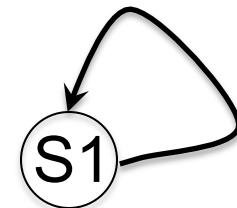


S117

Intel Nehalem
Compiler report: Loop was vectorized
Exec. Time scalar code: 6.0
Exec. Time vector code: 2.7
Speedup: 2.2

S118

```
for (int i=1;i<LEN;i++){  
S1  a[i]=a[i-1]+b[i];  
}
```



S118

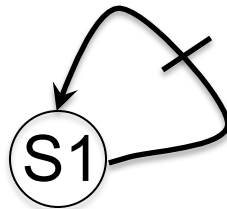
Intel Nehalem
Compiler report: Loop was not vectorized. Existence of vector dependence
Exec. Time scalar code: 7.2
Exec. Time vector code: --
Speedup: --



Cycles in the DG (III)

S117

```
for (int i=0;i<LEN-1;i++){  
S1  a[i]=a[i+1]+b[i];  
}
```



S117

IBM Power 7

Compiler report: Loop was SIMD vectorized

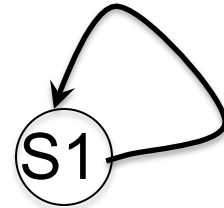
Exec. Time scalar code: 2.0

Exec. Time vector code: 1.0

Speedup: 2.0

S118

```
for (int i=1;i<LEN;i++){  
S1  a[i]=a[i-1]+b[i];  
}
```



S118

IBM Power 7

Compiler report: : Loop was not SIMD vectorized because a data dependence prevents SIMD vectorization

Exec. Time scalar code: 7.2

Exec. Time vector code: --

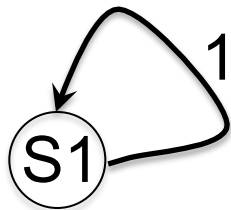
Speedup: --



Cycles in the DG (IV)

```
for (int i=1;i<LEN;i++){
S1  a[i]=a[i-1]+b[i];
}
```

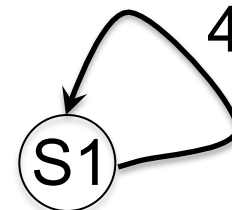
$a[1]=a[0]+b[1]$
 $a[2]=a[1]+b[2]$
 $a[3]=a[2]+b[3]$



Self true-dependence
is **not** vectorized

```
for (int i=4;i<LEN;i++){
  a[i]=a[i-4]+b[i];
}
```

$i=4$ $a[4]=a[0]+b[4]$
 $i=5$ $a[5]=a[1]+b[5]$
 $i=6$ $a[6]=a[2]+b[6]$
 $i=7$ $a[7]=a[3]+b[7]$
 $i=8$ $a[8]=a[4]+b[8]$
 $i=9$ $a[9]=a[5]+b[9]$
 $i=10$ $a[10]=a[6]+b[10]$
 $i=11$ $a[11]=a[7]+b[11]$



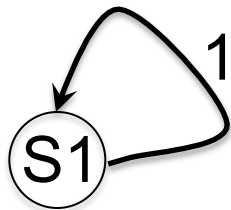
This is also a self-true
dependence. But ...
can it be vectorized?



Cycles in the DG (IV)

```
for (int i=1;i<n;i++){
S1  a[i]=a[i-1]+b[i];
}
```

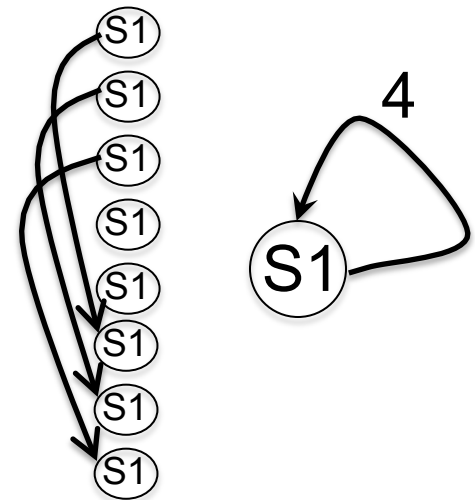
$a[1]=a[0]+b[1]$
 $a[2]=a[1]+b[2]$
 $a[3]=a[2]+b[3]$



Self true-dependence
cannot be vectorized

```
for (int i=4;i<LEN;i++){
  a[i]=a[i-4]+b[i];
}
```

$i=4 \quad a[4] = a[0]+b[4]$
 $i=5 \quad a[5] = a[1]+b[5]$
 $i=6 \quad a[6] = a[2]+b[6]$
 $i=7 \quad a[7] = a[3]+b[7]$
 $i=8 \quad a[8] = a[4]+b[8]$
 $i=9 \quad a[9] = a[5]+b[9]$
 $i=10 \quad a[10] = a[6]+b[10]$
 $i=11 \quad a[11] = a[7]+b[11]$



Yes, it can be vectorized because the dependence distance is 4, which is the number of iterations that the SIMD unit can execute simultaneously.



Cycles in the DG (IV)

S119

```
for (int i=4;i<LEN;i++){  
    a[i]=a[i-4]+b[i];  
}
```

Intel Nehalem

Compiler report: Loop was vectorized

Exec. Time scalar code: 8.4

Exec. Time vector code: 3.9

Speedup: 2.1

IBM Power 7

Compiler report: Loop was SIMD vectorized

Exec. Time scalar code: 6.6

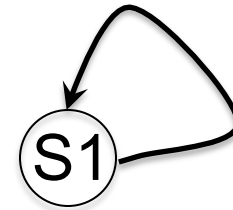
Exec. Time vector code: 1.8

Speedup: 3.7



Cycles in the DG (V)

```
    for (int i = 0; i < LEN-1; i++) {  
        for (int j = 0; j < LEN; j++)  
S1      a[i+1][j] = a[i][j] + b;  
    }
```



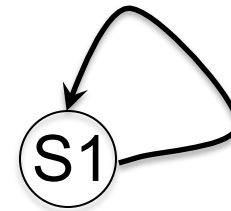
Can this loop be vectorized?

```
i=0, j=0: a[1][0] = a[0][0] + b  
          j=1: a[1][1] = a[0][1] + b  
          j=2: a[1][2] = a[0][2] + b  
i=1  j=0: a[2][0] = a[1][0] + b  
          j=1: a[2][1] = a[1][1] + b  
          j=2: a[2][2] = a[1][2] + b
```



Cycles in the DG (V)

```
for (int i = 0; i < LEN-1; i++) {  
    for (int j = 0; j < LEN; j++)  
S1      a[i+1][j] = a[i][j] + (float) 1.0;  
}
```



Can this loop be vectorized?

i=0, j=0: a[1][0] = a[0][0] + 1
j=1: a[1][1] = a[0][1] + 1
j=2: a[1][2] = a[0][2] + 1
i=1 j=0: a[2][0] = a[1][0] + 1
j=1: a[2][1] = a[1][1] + 1
j=2: a[2][2] = a[1][2] + 1

Diagram showing data dependencies between iterations. Arrows point from a[1][0] to a[2][0], a[1][1] to a[2][1], and a[1][2] to a[2][2], illustrating that the inner loop of iteration i=1 depends on the inner loop of iteration i=0.

Dependences occur in the outermost loop.

- outer loop runs serially

- inner loop can be vectorized

```
for (int i=0;i<LEN;i++){  
    a[i+1][0:LEN-1]=a[i][0:LEN-1]+b;  
}
```



Cycles in the DG (V)

S121

```
for (int i = 0; i < LEN-1; i++) {  
    for (int j = 0; j < LEN; j++)  
        a[i+1][j] = a[i][j] + 1;  
}
```

Intel Nehalem

Compiler report: Loop was
vectorized

Exec. Time scalar code: 11.6

Exec. Time vector code: 3.2

Speedup: 3.5

IBM Power 7

Compiler report: Loop was SIMD
vectorized

Exec. Time scalar code: 3.9

Exec. Time vector code: 1.8

Speedup: 2.1

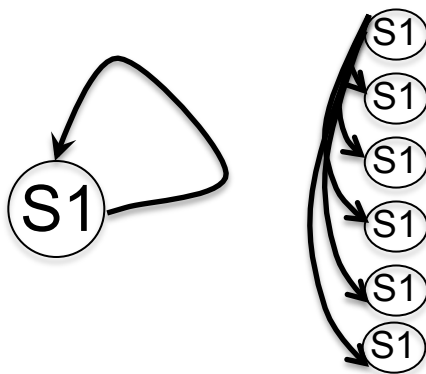


Cycles in the DG (VI)

- Cycles can appear because the compiler does not know if there are dependences

```
for (int i=0;i<LEN;i++){  
S1  a[r[i]] = a[r[i]] * (float) 2.0;  
}
```

Is there a value of i such
that $r[i'] = r[i]$, such that $i' \neq i$?



Compiler cannot resolve the system

To be safe, it considers that a data dependence is possible for every instance of S1



Cycles in the DG (VI)

- The compiler is conservative.
- The compiler only vectorizes when it can prove that it is safe to do it.

```
for (int i=0;i<LEN;i++){  
    r[i] = i;  
    a[r[i]] = a[r[i]]* (float) 2.0;  
}
```

Does the compiler use the info that $r[i] = i$ to compute data dependences?



Cycles in the DG (VI)

S122

```
for (int i=0;i<LEN;i++){  
    a[r[i]]=a[r[i]]*(float)2.0;  
}
```

S123

```
for (int i=0;i<LEN;i++){  
    r[i] = i;  
    a[r[i]]=a[r[i]]*(float)2.0;  
}
```

Does the compiler use the info that $r[i] = i$ to compute data dependences?

S122

Intel Nehalem

Compiler report: Loop was not vectorized. Existence of vector dependence

Exec. Time scalar code: 5.0

Exec. Time vector code: --

Speedup: --

S123

Intel Nehalem

Compiler report: Partial Loop was vectorized

Exec. Time scalar code: 5.8

Exec. Time vector code: 5.7

Speedup: 1.01



Cycles in the DG (VI)

S122

```
for (int i=0;i<LEN;i++){  
    a[r[i]]=a[r[i]]*(float)2.0;  
}
```

S123

```
for (int i=0;i<LEN;i++){  
    r[i] = i;  
    a[r[i]]=a[r[i]]*(float)2.0;  
}
```

Does the compiler use the info that $r[i] = i$ to compute data dependences?

S122

IBM Power 7

Compiler report: Loop was not vectorized because a data dependence prevents SIMD vectorization

Exec. Time scalar code: 2.6

Exec. Time vector code: 2.3

Speedup: 1.1

S123

IBM Power 7

Compiler report: Loop was SIMD vectorized

Exec. Time scalar code: 2.1

Exec. Time vector code: 0.9

Speedup: 2.3



Dependence Graphs and Compiler Vectorization

- No dependences: Vectorized by the compiler
- Acyclic graphs:
 - All dependences are forward:
 - Vectorized by the compiler
 - Some backward dependences:
 - Sometimes vectorized by the compiler
- Cycles in the dependence graph
 - Self-antidependence:
 - Vectorized by the compiler
 - Recurrence:
 - Usually not vectorized by the the compiler
 - Other examples



Loop Transformations

- Compiler Directives
- Loop Distribution or loop fission
- Reordering Statements
- Node Splitting
- Scalar expansion
- Loop Peeling
- Loop Fusion
- Loop Unrolling
- Loop Interchanging



Compiler Directives (I)

- When the compiler does not vectorize automatically due to dependences the programmer can inform the compiler that it is safe to vectorize:

`#pragma ivdep (ICC compiler)`

`#pragma ibm independent_loop (XLC compiler)`

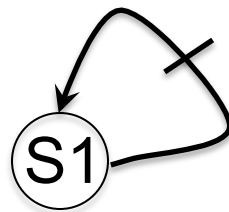


Compiler Directives (I)

- This loop can be vectorized when $k < -3$ and $k \geq 0$.
- Programmer knows that $k \geq 0$

```
for (int i=val; i<LEN-k; i++)  
    a[i]=a[i+k]+b[i];
```

If ($k \geq 0$) \rightarrow no dependence
or self-anti-dependence

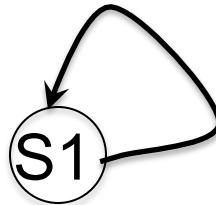


$k = 1$

$a[0] = a[1] + b[0]$
 $a[1] = a[2] + b[1]$
 $a[2] = a[3] + b[2]$

Can
be vectorized

If ($k < 0$) \rightarrow self-true dependence



$k = -1$

$a[1] = a[0] + b[0]$
 $a[2] = a[1] + b[1]$
 $a[3] = a[2] + b[2]$

Cannot
be vectorized



Compiler Directives (I)

- This loop can be vectorized when $k < -3$ and $k \geq 0$.
- Programmer knows that $k \geq 0$

How can the programmer tell the compiler that $k \geq 0$

```
for (int i=val; i<LEN-k; i++)  
    a[i]=a[i+k]+b[i];
```



Compiler Directives (I)

- This loop can be vectorized when $k < -3$ and $k \geq 0$.
- Programmer knows that $k \geq 0$

Intel ICC provides the `#pragma ivdep` to tell the compiler that it is safe to ignore unknown dependences

```
#pragma ivdep  
for (int i=val; i<LEN-k; i++)  
    a[i]=a[i+k]+b[i];
```

wrong results will be obtained if loop is vectorized when $-3 < k < 0$



Compiler Directives (I)

S124

```
for (int i=0;i<LEN-k;i++)  
    a[i]=a[i+k]+b[i];
```

S124_1

```
if (k>=0)  
    for (int i=0;i<LEN-k;i++)  
        a[i]=a[i+k]+b[i];  
if (k<0)  
    for (int i=0;i<LEN-k;i++)  
        a[i]=a[i+k]+b[i];
```

S124_2

```
if (k>=0)  
    #pragma ivdep  
    for (int i=0;i<LEN-k;i++)  
        a[i]=a[i+k]+b[i];  
if (k<0)  
    for (int i=0;i<LEN-k;i++)  
        a[i]=a[i+k]+b[i];
```

S124 and S124_1

Intel Nehalem

Compiler report: Loop was not vectorized. Existence of vector dependence

Exec. Time scalar code: 6.0

Exec. Time vector code: --

Speedup: --

S124_2

Intel Nehalem

Compiler report: Loop was vectorized

Exec. Time scalar code: 6.0

Exec. Time vector code: 2.4

Speedup: 2.5



Compiler Directives (I)

S124

```
for (int i=0;i<LEN-k;i++) if (k>=0)
    a[i]=a[i+k]+b[i];
```

S124_1

```
for (int i=0;i<LEN-k;i++)
    a[i]=a[i+k]+b[i];
if (k<0)
    for (int i=0;i<LEN-k;i++)
        a[i]=a[i+k]+b[i];
```

S124_2

```
if (k>=0)
    #pragma ibm independent_loop
    for (int i=0;i<LEN-k;i++)
        a[i]=a[i+k]+b[i];
if (k<0)
    for (int i=0;i<LEN-k;i++)
        a[i]=a[i+k]+b[i];
```

S124 and S124_1

IBM Power 7

Compiler report: Loop was not vectorized because a data dependence prevents SIMD vectorization

Exec. Time scalar code: 2.2

Exec. Time vector code: --

Speedup: --

S124_2

#pragma ibm independent_loop
needs AIX OS (we ran the experiments on Linux)



Compiler Directives (II)

- Programmer can disable vectorization of a loops when the when the vector code runs slower than the scalar code

`#pragma novector (ICC compiler)`

`#pragma nosimd (XLC compiler)`

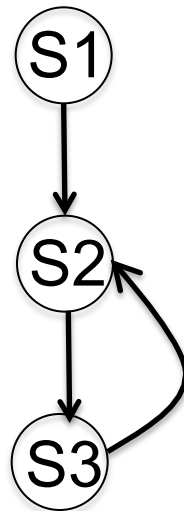


Compiler Directives (II)

Vector code can run slower than scalar code

```
for (int i=1;i<LEN;i++){  
S1  a[i] = b[i] + c[i];  
S2  d[i] = a[i] + e[i-1];  
S3  e[i] = d[i] + c[i];  
}
```

Less locality when
executing in vector mode



S1 can be vectorized
S2 and S3 cannot be vectorized (as they are)



Compiler Directives (II)

S116

```
#pragma novector
```

```
for (int i=1;i<LEN;i++){  
    a[i] = b[i] + c[i];  
    d[i] = a[i] + e[i-1];  
    e[i] = d[i] + c[i];  
}
```

S116

Intel Nehalem

Compiler report: Loop was
partially vectorized

Exec. Time scalar code: 14.7

Exec. Time vector code: 18.1

Speedup: 0.8



Loop Distribution

- It is also called loop fission.
- Divides loop control over different statements in the loop body.

```
for (i=1; i<LEN; i++) {  
    a[i]= (float)sqrt(b[i])+  
          (float)sqrt(c[i]);  
    dummy(a,b,c);  
}  
→  
for (i=1; i<LEN; i++)  
    a[i]= (float)sqrt(b[i])+  
          (float)sqrt(c[i]);  
  
for (i=1; i<LEN; i++)  
    dummy(a,b,c);
```

- Compiler cannot analyze the dummy function.
As a result, the compiler cannot apply loop distribution,
because it does not know if it is a legal transformation
- Programmer can apply loop distribution if legal.



Loop Distribution

S126

```
for (i=1; i<LEN; i++) {  
    a[i]= (float)sqrt(b[i])+  
          (float)sqrt(c[i]);  
    dummy(a,b,c);  
}
```

S126_1

```
for (i=1; i<LEN; i++)  
    a[i]= (float)sqrt(b[i])+  
          (float)sqrt(c[i]);  
for (i=1; i<LEN; i++)  
    dummy(a,b,c);
```

S126

Intel Nehalem

Compiler report: Loop was not vectorized

Exec. Time scalar code: 4.3

Exec. Time vector code: --

Speedup: --

S126_1

Intel Nehalem

Compiler report:

- Loop 1 was vectorized.
- Loop 2 was not vectorized

Exec. Time scalar code: 5.1

Exec. Time vector code: 1.1

Speedup: 4.6



Loop Distribution

S126

```
for (i=1; i<LEN; i++) {  
    a[i]= (float)sqrt(b[i])+  
          (float)sqrt(c[i]);  
    dummy(a,b,c);  
}
```

S126_1

```
for (i=1; i<LEN; i++)  
    a[i]= (float)sqrt(b[i])+  
          (float)sqrt(c[i]);  
for (i=1; i<LEN; i++)  
    dummy(a,b,c);
```

S126

IBM Power 7

Compiler report: Loop was not
SIMD vectorized

Exec. Time scalar code: 1.3

Exec. Time vector code: --

Speedup: --

S126_1

IBM Power 7

Compiler report:

- Loop 1 was SIMD vectorized.

- Loop 2 was not SIMD vectorized

Exec. Time scalar code: 1.14

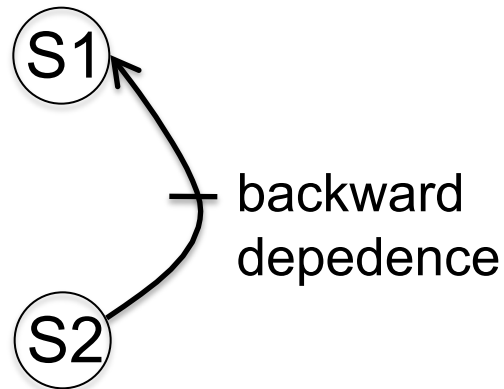
Exec. Time vector code: 1.0

Speedup: 1.14

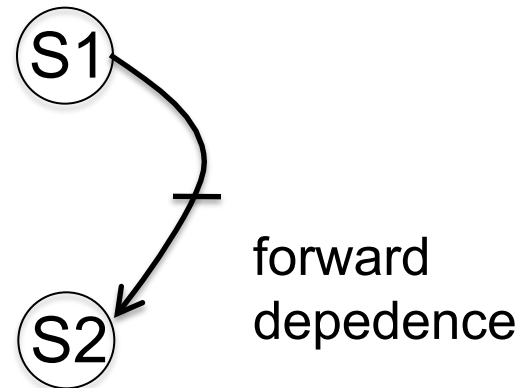


Reordering Statements

```
for (i=0; i<LEN; i++) {  
S1  a[i]= b[i] + c[i];  
S2  d[i] = a[i+1]+(float)1.0;  
}
```



```
for (i=0; i<LEN; i++) {  
S1  d[i] = a[i+1]+(float)1.0;  
S2  a[i]= b[i] + c[i];  
}
```



Reordering Statements

S114

```
for (i=0; i<LEN; i++) {  
    a[i]= b[i] + c[i];  
    d[i] = a[i+1]+(float)1.0;  
}
```

S114_1

```
for (i=0; i<LEN; i++) {  
    d[i] = a[i+1]+(float)1.0;  
    a[i]= b[i] + c[i];  
}
```

S114

Intel Nehalem

Compiler report: Loop was not vectorized. Existence of vector dependence

Exec. Time scalar code: 12.6

Exec. Time vector code: --

Speedup: --

S114_1

Intel Nehalem

Compiler report: Loop was vectorized.

Exec. Time scalar code: 10.7

Exec. Time vector code: 9.4

Speedup: 1.03



Reordering Statements

S114

```
for (i=0; i<LEN; i++) {  
    a[i]= b[i] + c[i];  
    d[i] = a[i+1]+(float)1.0;  
}
```

S114_1

```
for (i=0; i<LEN; i++) {  
    d[i] = a[i+1]+(float)1.0;  
    a[i]= b[i] + c[i];  
}
```

The IBM XLC compiler generated the same code in both cases

S114

IBM Power 7

Compiler report: Loop was SIMD
vectorized

Exec. Time scalar code: 3.3

Exec. Time vector code: 1.8

Speedup: 1.8

S114_1

IBM Power 7

Compiler report: Loop was SIMD
vectorized

Exec. Time scalar code: 3.3

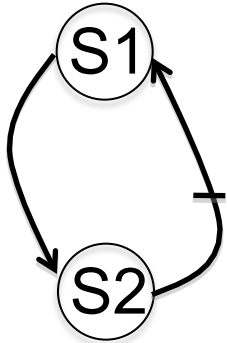
Exec. Time vector code: 1.8

Speedup: 1.8

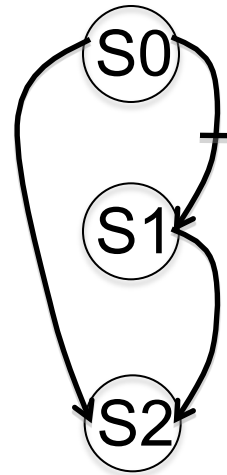


Node Splitting

```
for (int i=0;i<LEN-1;i++){  
S1  a[i]=b[i]+c[i];  
S2  d[i]=(a[i]+a[i+1])*(float)0.5;  
}
```



```
for (int i=0;i<LEN-1;i++){  
S0 temp[i]=a[i+1];  
S1 a[i]=b[i]+c[i];  
S2 d[i]=(a[i]+temp[i])*(float) 0.5;  
}
```



Node Splitting

S126

```
for (int i=0;i<LEN-1;i++){  
    a[i]=b[i]+c[i];  
    d[i]=(a[i]+a[i+1])*(float)0.5;  
}
```

S126_1

```
for (int i=0;i<LEN-1;i++){  
    temp[i]=a[i+1];  
    a[i]=b[i]+c[i];  
    d[i]=(a[i]+temp[i])*(float)0.5;  
}
```

S126

Intel Nehalem

Compiler report: Loop was not vectorized. Existence of vector dependence

Exec. Time scalar code: 12.6

Exec. Time vector code: --

Speedup: --

S126_1

Intel Nehalem

Compiler report: Loop was vectorized.

Exec. Time scalar code: 13.2

Exec. Time vector code: 9.7

Speedup: 1.3



Node Splitting

S126

```
for (int i=0;i<LEN-1;i++){  
S1  a[i]=b[i]+c[i];  
S2  d[i]=(a[i]+a[i+1])*(float)0.5;  
}
```

S126_1

```
for (int i=0;i<LEN-1;i++){  
S0 temp[i]=a[i+1];  
S1 a[i]=b[i]+c[i];  
S2 d[i]=(a[i]+temp[i])*(float) 0.5  
}
```

S126

IBM Power 7

Compiler report: Loop was SIMD
vectorized

Exec. Time scalar code: 3.8

Exec. Time vector code: 1.7

Speedup: 2.2

S126_1

IBM Power 7

Compiler report: Loop was SIMD
vectorized

Exec. Time scalar code: 5.1

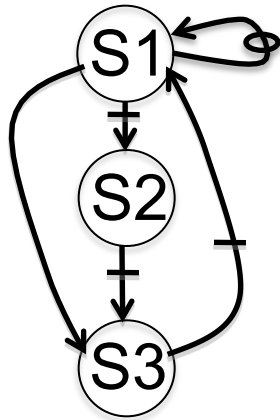
Exec. Time vector code: 2.4

Speedup: 2.0

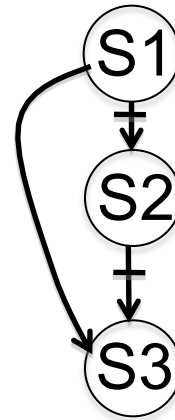


Scalar Expansion

```
for (int i=0;i<n;i++){  
  S1  t = a[i];  
  S2  a[i] = b[i];  
  S3  b[i] = t;  
}
```



```
for (int i=0;i<n;i++){  
  S1  t[i] = a[i];  
  S2  a[i] = b[i];  
  S3  b[i] = t[i];  
}
```



Scalar Expansion

S139

```
for (int i=0;i<n;i++){  
    t = a[i];  
    a[i] = b[i];  
    b[i] = t;  
}
```

S139_1

```
for (int i=0;i<n;i++){  
    t[i] = a[i];  
    a[i] = b[i];  
    b[i] = t[i];  
}
```

S139

Intel Nehalem

Compiler report: Loop was vectorized.

Exec. Time scalar code: 0.7

Exec. Time vector code: 0.4

Speedup: 1.5

S139_1

Intel Nehalem

Compiler report: Loop was vectorized.

Exec. Time scalar code: 0.7

Exec. Time vector code: 0.4

Speedup: 1.5



Scalar Expansion

S139

```
for (int i=0;i<n;i++){  
    t = a[i];  
    a[i] = b[i];  
    b[i] = t;  
}
```

S139_1

```
for (int i=0;i<n;i++){  
    t[i] = a[i];  
    a[i] = b[i];  
    b[i] = t[i];  
}
```

S139

IBM Power 7

Compiler report: Loop was SIMD
vectorized

Exec. Time scalar code: 0.28

Exec. Time vector code: 0.14

Speedup: 2

S139_1

IBM Power 7

Compiler report: Loop was SIMD
vectorized

Exec. Time scalar code: 0.28

Exec. Time vector code: 0.14

Speedup: 2.0



Loop Peeling

- Remove the first/s or the last/s iteration of the loop into separate code outside the loop
- It is always legal, provided that no additional iterations are introduced.
- When the trip count of the loop is not constant the peeled loop has to be protected with additional runtime tests.
- This transformation is useful to enforce a particular initial memory alignment on array references prior to loop vectorization.

```
for (i=0; i<LEN; i++)  
    A[i] = B[i] + C[i];
```

→

```
A[0] = B[0] + C[0];  
for (i=1; i<LEN; i++)  
    A[i] = B[i] + C[i];
```



Loop Peeling

- Remove the first/s or the last/s iteration of the loop into separate code outside the loop
- It is always legal, provided that no additional iterations are introduced.
- When the trip count of the loop is not constant the peeled loop has to be protected with additional runtime tests.
- This transformation is useful to enforce a particular initial memory alignment on array references prior to loop vectorization.

```
for (i=0; i<LEN; i++)  
    A[i] = B[i] + C[i];
```

→

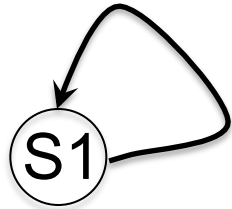
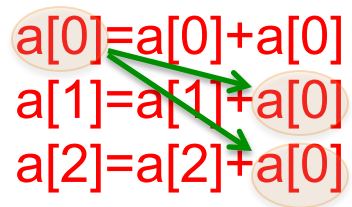
```
if (N>=1)  
    A[0] = B[0] + C[0];  
for (i=1; i<LEN; i++)  
    A[i] = B[i] + C[i];
```



Loop Peeling

```
for (int i=0;i<LEN;i++){  
S1  a[i] = a[i] + a[0];  
}
```

$a[0] = a[0] + a[0]$
 $a[1] = a[1] + a[0]$
 $a[2] = a[2] + a[0]$



Self true-dependence
is **not** vectorized

```
a[0] = a[0] + a[0];  
for (int i=1;i<LEN;i++){  
  a[i] = a[i] + a[0]  
}
```

After loop peeling, there are no
dependences, and the loop can be
vectorized



Loop Peeling

S127

```
for (int i=0;i<LEN;i++){  
S1  a[i] = a[i] + a[0];  
}
```

S127_1

```
a[0]= a[0] + a[0];  
for (int i=1;i<LEN;i++){  
  a[i] = a[i] + a[0]  
}
```

S127

Intel Nehalem

Compiler report: Loop was not vectorized. Existence of vector dependence

Exec. Time scalar code: 6.7

Exec. Time vector code: --

Speedup: --

S127_1

Intel Nehalem

Compiler report: Loop was vectorized.

Exec. Time scalar code: 6.6

Exec. Time vector code: 1.2

Speedup: 5.2



Loop Peeling

S127

```
for (int i=0;i<LEN;i++)  
{  
    a[i] = a[i] + a[0];  
}
```

S127_1

```
a[0]= a[0] + a[0];  
for (int i=1;i<LEN;i++)  
{  
    a[i] = a[i] + a[0];  
}
```

S127_2

```
a[0]= a[0] + a[0];  
float t = a[0];  
for (int i=1;i<LEN;i++)  
{  
    a[i] = a[i] + t;  
}
```

S127

IBM Power 7
Compiler report: Loop
was not SIMD vectorized
Time scalar code: 2.4
Time vector code: --
Speedup: --

S127_1

IBM Power 7
Compiler report: Loop
was not SIMD vectorized
Exec. scalar code: 2.4
Exec. vector code: --
Speedup: --

S127_2

IBM Power 7
Compiler report: Loop
was vectorized
Exec. scalar code: 1.58
Exec. vector code: 0.62
Speedup: 2.54



Loop Interchanging

- This transformation switches the positions of one loop that is tightly nested within another loop.

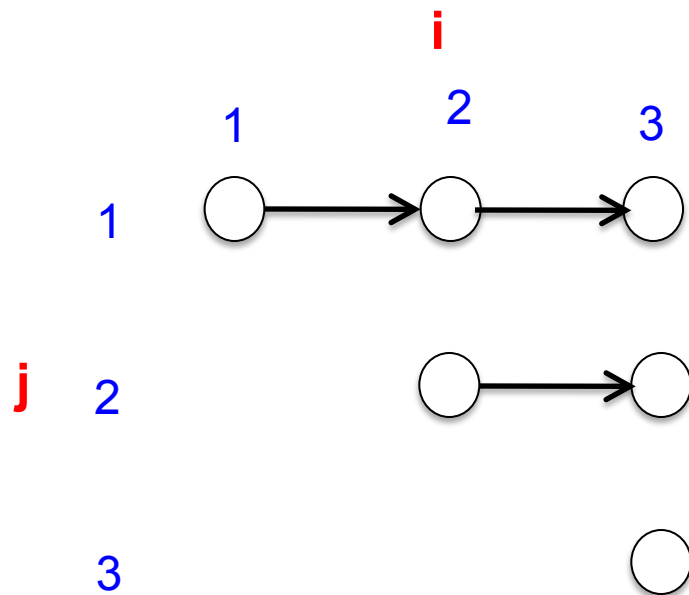
```
for (i=0; i<LEN; i++)  
  for (j=0; j<LEN; j++)  
    A[i][j]=0.0;
```

```
for (j=0; j<LEN; j++)  
  for (i=0; i<LEN; i++)  
    A[i][j]=0.0;
```



Loop Interchanging

```
for (j=1; j<LEN; j++){
  for (i=j; i<LEN; i++){
    A[i][j]=A[i-1][j]+(float) 1.0;
  }
}
```



$j=1 \begin{cases} i=1 & A[1][1]=A[0][1] + 1 \\ i=2 & A[2][1]=A[1][1] + 1 \\ i=3 & A[3][1]=A[2][1] + 1 \end{cases}$

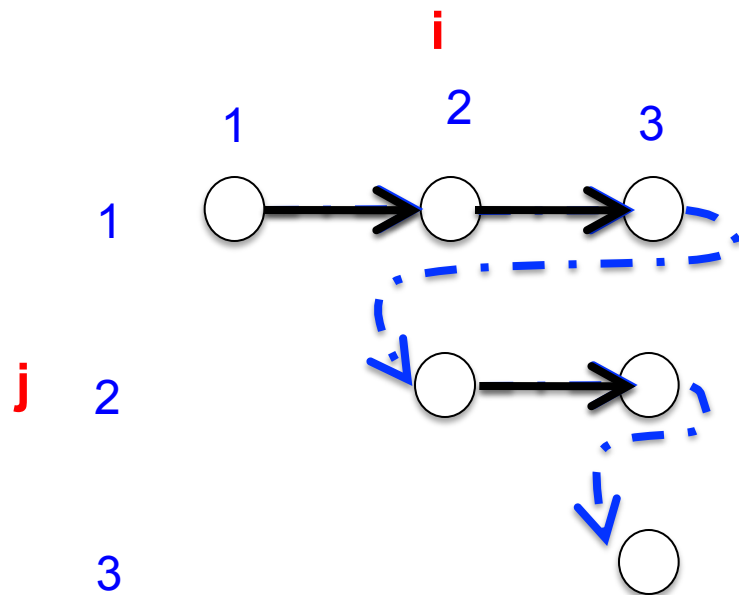
$j=2 \begin{cases} i=2 & A[2][2]=A[1][2] + 1 \\ i=3 & A[3][2]=A[2][2] + 1 \end{cases}$

$j=3 \quad i=3 \quad A[3][3]=A[2][3] + 1$



Loop Interchanging

```
for (j=1; j<LEN; j++){
  for (i=j; i<LEN; i++){
    A[i][j]=A[i-1][j]+(float) 1.0;
  }
}
```



$j=1 \begin{cases} i=1 & A[1][1] = A[0][1] + 1 \\ i=2 & A[2][1] = A[1][1] + 1 \\ i=3 & A[3][1] = A[2][1] + 1 \end{cases}$

$j=2 \begin{cases} i=2 & A[2][2] = A[1][2] + 1 \\ i=3 & A[3][2] = A[2][2] + 1 \end{cases}$

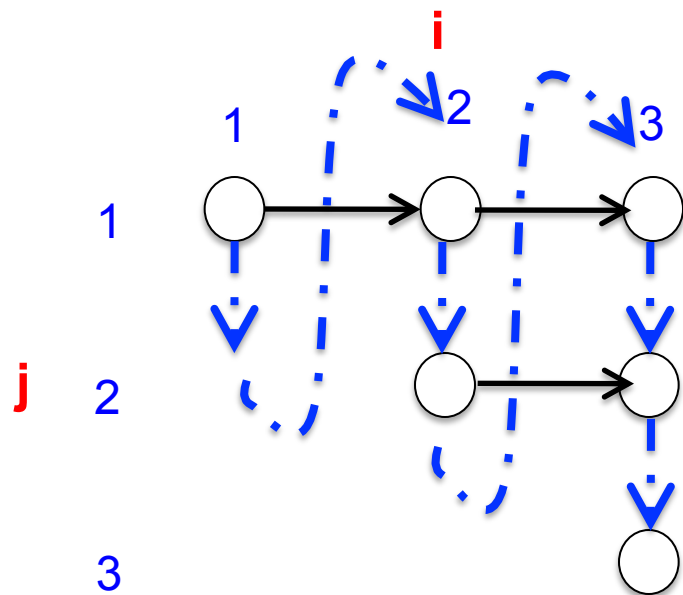
$j=3 \quad i=3 \quad A[3][3] = A[2][3] + 1$

Inner loop cannot be vectorized
because of self-dependence



Loop Interchanging

```
for (i=1; i<LEN; i++){
  for (j=1; j<i+1; j++){
    A[i][j]=A[i-1][j]+(float) 1.0;
  }
}
```



$i=1 \quad \left\{ \begin{array}{l} j=1 \quad A[1][1]=A[0][1] + 1 \end{array} \right.$

$i=2 \quad \left\{ \begin{array}{l} j=1 \quad A[2][1]=A[1][1] + 1 \\ j=2 \quad A[2][2]=A[1][2] + 1 \end{array} \right.$

$i=3 \quad \left\{ \begin{array}{l} j=1 \quad A[3][1]=A[2][1] + 1 \\ j=2 \quad A[3][2]=A[2][2] + 1 \\ j=3 \quad A[3][3]=A[2][3] + 1 \end{array} \right.$

Loop interchange is legal
No dependences in inner loop



Loop Interchanging

S228

```
for (j=1; j<LEN; j++){  
  for (i=j; i<LEN; i++){  
    A[i][j]=A[i-1][j]+(float)1.0;  
  }}
```

S228_1

```
for (i=1; i<LEN; i++){  
  for (j=1; j<i+1; j++){  
    A[i][j]=A[i-1][j]+(float)1.0;  
  }}
```

S228

Intel Nehalem

Compiler report: Loop was not vectorized.

Exec. Time scalar code: 2.3

Exec. Time vector code: --

Speedup: --

S228_1

Intel Nehalem

Compiler report: Loop was vectorized.

Exec. Time scalar code: 0.6

Exec. Time vector code: 0.2

Speedup: 3



Loop Interchanging

S228

```
for (j=1; j<LEN; j++){  
  for (i=j; i<LEN; i++){  
    A[i][j]=A[i-1][j]+(float)1.0;  
  }}
```

S228_1

```
for (i=1; i<LEN; i++){  
  for (j=1; j<i+1; j++){  
    A[i][j]=A[i-1][j]+(float)1.0;  
  }}
```

S228

IBM Power 7

Compiler report: Loop was not
SIMD vectorized

Exec. Time scalar code: 0.5

Exec. Time vector code: --

Speedup: --

S228_1

IBM Power 7

Compiler report: Loop was SIMD
vectorized

Exec. Time scalar code: 0.2

Exec. Time vector code: 0.14

Speedup: 1.42



Outline

1. Intro
2. Data Dependences (Definition)
3. Overcoming limitations to SIMD-Vectorization
 - Data Dependences
 - Reductions
 - Data Alignment
 - Aliasing
 - Non-unit strides
 - Conditional Statements
4. Vectorization using intrinsics

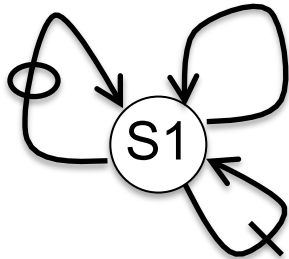


Reductions

- Reduction is an operation, such as addition, which is applied to the elements of an array to produce a result of a lesser rank.

Sum Reduction

```
sum = 0;  
for (int i=0; i<LEN; ++i){  
    sum += a[i];  
}
```



Max Loc Reduction

```
x = a[0];  
index = 0;  
for (int i=0; i<LEN; ++i){  
    if (a[i] > x) {  
        x = a[i];  
        index = i;  
    }  
}
```



Reductions

S131

```
sum =0;
for (int i=0;i<LEN;++i){
    sum+= a[i];
}
```

S132

```
x = a[0];
index = 0;
for (int i=0;i<LEN;++i){
    if (a[i] > x) {
        x = a[i];
        index = i;
    }
}
```

S131

Intel Nehalem
Compiler report: Loop was vectorized.
Exec. Time scalar code: 5.2
Exec. Time vector code: 1.2
Speedup: 4.1

S132

Intel Nehalem
Compiler report: Loop was vectorized.
Exec. Time scalar code: 9.6
Exec. Time vector code: 2.4
Speedup: 3.9



Reductions

S131

```
sum =0;
for (int i=0;i<LEN;++i){
    sum+= a[i];
}
```

S131

IBM Power 7

Compiler report: Loop was SIMD
vectorized

Exec. Time scalar code: 1.1

Exec. Time vector code: 0.4

Speedup: 2.4

S132

```
x = a[0];
index = 0;
for (int i=0;i<LEN;++i){
    if (a[i] > x) {
        x = a[i];
        index = i;
    }
}
```

S132

IBM Power 7

Compiler report: Loop was not
SIMD vectorized

Exec. Time scalar code: 4.4

Exec. Time vector code: --

Speedup: --



Reductions

S141_1

```
for (int i = 0; i < 64; i++){
    max[i] = a[i];
    loc[i] = i; }
for (int i = 0; i < LEN; i+=64){
    for (int j=0, k=i; k<i+64; k++,j++)
    {
        int cmp = max[j] < a[k];
        max[j] = cmp ? a[k] : max[j];
        loc[j] = cmp ? k : loc[j];
    } }
MAX = max[0];
LOC = 0;
for (int i = 0; i < 64; i++){
    if (MAX < max[i]){
        MAX = max[i];
        LOC = loc[i];
    } }
```

S141_1

IBM Power 7

Compiler report: Loop was SIMD
vectorized

Exec. Time scalar code: 10.2

Exec. Time vector code: 2.7

Speedup: 3.7

S141_2

IBM Power 7

**A version written with intrinsics
runs in 1.6 secs.**



Outline

1. Intro
2. Data Dependences (Definition)
3. Overcoming limitations to SIMD-Vectorization
 - Data Dependences
 - Induction variables
 - Data Alignment
 - Aliasing
 - Non-unit strides
 - Conditional Statements
4. Vectorization with intrinsics

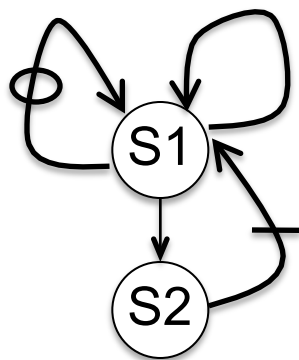


Induction variables

- Induction variable is a variable that can be expressed as a function of the loop iteration variable

```
float s = (float)0.0;  
for (int i=0;i<LEN;i++){  
    s += (float)2.;  
    a[i] = s * b[i];  
}
```

```
for (int i=0;i<LEN;i++){  
    a[i] = (float)2.*(i+1)*b[i];  
}
```



Induction variables

S133

```
float s = (float)0.0;  
for (int i=0;i<LEN;i++){  
    s += (float)2.;  
    a[i] = s * b[i];  
}
```

S133_1

```
for (int i=0;i<LEN;i++){  
    a[i] = (float)2.*(i+1)*b[i];  
}
```

The Intel ICC compiler generated the same vector code in both cases

S133

Intel Nehalem
Compiler report: Loop was vectorized.
Exec. Time scalar code: 6.1
Exec. Time vector code: 1.9
Speedup: 3.1

S133_1

Intel Nehalem
Compiler report: Loop was vectorized.
Exec. Time scalar code: 8.4
Exec. Time vector code: 1.9
Speedup: 4.2



Induction variables

S133

```
float s = (float)0.0;
for (int i=0;i<LEN;i++){
    s += (float)2.;
    a[i] = s * b[i];
}
```

S133_1

```
for (int i=0;i<LEN;i++){
    a[i] = (float)2.*(i+1)*b[i];
}
```

S133

IBM Power 7

Compiler report: Loop was not SIMD vectorized

Exec. Time scalar code: 2.7

Exec. Time vector code: --

Speedup: --

S133_1

IBM Power 7

Compiler report: Loop was SIMD vectorized

Exec. Time scalar code: 3.7

Exec. Time vector code: 1.4

Speedup: 2.6



Induction Variables

- Coding style matters:

```
for (int i=0;i<LEN;i++) {  
    *a = *b + *c;  
    a++; b++; c++;  
}
```

```
for (int i=0;i<LEN;i++){  
    a[i] = b[i] + c[i];  
}
```

These codes are equivalent, but ...



Induction Variables

S134

```
for (int i=0;i<LEN;i++) {  
    *a = *b + *c;  
    a++; b++; c++;  
}
```

S134_1

```
for (int i=0;i<LEN;i++){  
    a[i] = b[i] + c[i];  
}
```

S134

Intel Nehalem

Compiler report: Loop was not vectorized.

Exec. Time scalar code: 5.5

Exec. Time vector code: --

Speedup: --

S134_1

Intel Nehalem

Compiler report: Loop was vectorized.

Exec. Time scalar code: 6.1

Exec. Time vector code: 3.2

Speedup: 1.8



Induction Variables

S134

```
for (int i=0;i<LEN;i++) {  
    *a = *b + *c;  
    a++; b++; c++;  
}
```

S134_1

```
for (int i=0;i<LEN;i++){  
    a[i] = b[i] + c[i];  
}
```

The IBM XLC compiler generated the same code in both cases

S134

IBM Power 7

Compiler report: Loop was SIMD vectorized

Exec. Time scalar code: 2.2

Exec. Time vector code: 1.0

Speedup: 2.2

S134_1

IBM Power 7

Compiler report: Loop was SIMD vectorized

Exec. Time scalar code: 2.2

Exec. Time vector code: 1.0

Speedup: 2.2



Outline

1. Intro
2. Data Dependences (Definition)
3. Overcoming limitations to SIMD-Vectorization
 - Data Dependences
 - **Data Alignment**
 - Aliasing
 - Non-unit strides
 - Conditional Statements
4. Vectorization with intrinsics

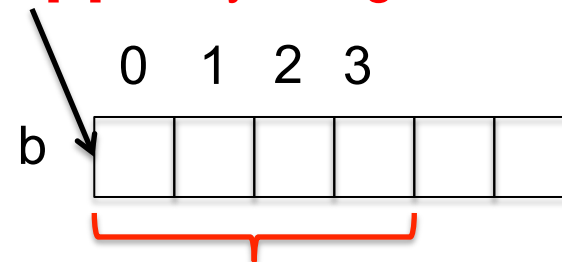


Data Alignment

- Vector loads/stores load/store 128 consecutive bits to a vector register.
- Data addresses need to be 16-byte (128 bits) aligned to be loaded/stored
 - Intel platforms support aligned and unaligned load/stores
 - IBM platforms do not support unaligned load/stores

```
void test1(float *a, float *b, float *c)
{
    for (int i=0; i<LEN; i++){
        a[i] = b[i] + c[i];
    }
}
```

Is &b[0] 16-byte aligned?



vector load loads b[0] ... b[3]



Data Alignment

- To know if a pointer is 16-byte aligned, the last digit of the pointer address in hex must be 0.
- Note that if &b[0] is 16-byte aligned, and is a single precision array, then &b[4] is also 16-byte aligned

```
__attribute__((aligned(16))) float B[1024];
```

```
int main(){  
    printf("%p, %p\n", &B[0], &B[4]);  
}
```

Output:

0x7fff1e9d8580, 0x7fff1e9d8590



Data Alignment

- In many cases, the compiler cannot statically know the alignment of the address in a pointer
- The compiler assumes that the base address of the pointer is 16-byte aligned and adds a run-time checks for it
 - if the runtime check is false, then it uses another code (which may be scalar)



Data Alignment

- Manual 16-byte alignment can be achieved by forcing the base address to be a multiple of 16.

```
__attribute__((aligned(16))) float b[N];  
float* a = (float*) memalign(16, N*sizeof(float));
```

- When the pointer is passed to a function, the compiler should be aware of where the 16-byte aligned address of the array starts.

```
void func1(float *a, float *b,  
float *c) {  
    __assume_aligned(a, 16);  
    __assume_aligned(b, 16);  
    __assume_aligned(c, 16);  
    for (int i=0; i<LEN; i++) {  
        a[i] = b[i] + c[i];  
    }  
}
```



Data Alignment - Example

```
float A[N] __attribute__((aligned(16)));  
float B[N] __attribute__((aligned(16)));  
float C[N] __attribute__((aligned(16)));  
  
void test(){  
    for (int i = 0; i < N; i++){  
        C[i] = A[i] + B[i];  
    }  
}
```



Data Alignment - Example

```
float A[N] __attribute__((aligned(16)));  
float B[N] __attribute__((aligned(16)));  
float C[N] __attribute__((aligned(16)));
```

```
void test1(){  
    __m128 rA, rB, rC;  
    for (int i = 0; i < N; i+=4){  
        rA = _mm_load_ps(&A[i]);  
        rB = _mm_load_ps(&B[i]);  
        rC = _mm_add_ps(rA,rB);  
        _mm_store_ps(&C[i], rC);  
    }  
}
```

```
void test3(){  
    __m128 rA, rB, rC;  
    for (int i = 1; i < N-3; i+=4){  
        rA = _mm_loadu_ps(&A[i]);  
        rB = _mm_loadu_ps(&B[i]);  
        rC = _mm_add_ps(rA,rB);  
        _mm_storeu_ps(&C[i], rC);  
    }  
}
```

```
void test2(){  
    __m128 rA, rB, rC;  
    for (int i = 0; i < N; i+=4){  
        rA = _mm_loadu_ps(&A[i]);  
        rB = _mm_loadu_ps(&B[i]);  
        rC = _mm_add_ps(rA,rB);  
        _mm_storeu_ps(&C[i], rC);  
    }  
}
```

Nanosecond per iteration			
	Core 2 Duo	Intel i7	Power 7
Aligned	0.577	0.580	0.156
Aligned (unaligned ld)	0.689	0.581	0.241
Unaligned	2.176	0.629	0.243



Alignment in a struct

```
struct st{
    char A;
    int B[64];
    float C;
    int D[64];
};

int main(){
    st s1;
    printf("%p, %p, %p, %p\n", &s1.A, s1.B, &s1.C, s1.D);}
```

Output:

0x7ffe6765f00, 0x7ffe6765f04, 0x7ffe6766004, 0x7ffe6766008

- Arrays B and D are not 16-bytes aligned (see the address)




Alignment in a struct

```
struct st{
    char A;
    int B[64] __attribute__((aligned(16)));
    float C;
    int D[64] __attribute__((aligned(16)));
};

int main(){
    st s1;
    printf("%p, %p, %p, %p\n", &s1.A, s1.B, &s1.C, s1.D);}
```

Output:

0x7fff1e9d8580, 0x7fff1e9d8590, 0x7fff1e9d8690, 0x7fff1e9d86a0

- Arrays A and B are aligned to 16-bytes (notice the 0 in the 4 least significant bits of the address)
-  Compiler automatically does padding

Outline

1. Intro
2. Data Dependences (Definition)
3. Overcoming limitations to SIMD-Vectorization
 - Data Dependences
 - Data Alignment
 - **Aliasing**
 - Non-unit strides
 - Conditional Statements
4. Vectorization with intrinsics



Aliasing

- Can the compiler vectorize this loop?

```
void func1(float *a, float *b, float *c){  
    for (int i = 0; i < LEN; i++) {  
        a[i] = b[i] + c[i];  
    }  
}
```



Aliasing

- Can the compiler vectorize this loop?

```
float* a = &b[1];
```

```
...
```

```
void func1(float *a, float *b, float *c)
{
    for (int i = 0; i < LEN; i++)
        a[i] = b[i] + c[i];
}
```

```
b[1] = b[0] + c[0]
```

```
b[2] = b[1] + c[1]
```



Aliasing

- Can the compiler vectorize this loop?

```
float* a = &b[1];
```

```
...
```

```
void func1(float *a, float *b, float *c)
{
    for (int i = 0; i < LEN; i++)
        a[i] = b[i] + c[i];
}
```

a and b are aliasing

There is a self-true dependence

Vectorizing this loop would
be illegal



Aliasing

- To vectorize, the compiler needs to guarantee that the pointers are not aliased.
- When the compiler does not know if two pointer are alias, it still vectorizes, but needs to add up-to $O(n^2)$ run-time checks, where n is the number of pointers

When the number of pointers is large, the compiler may decide to not vectorize

```
void func1(float *a, float *b, float *c){  
    for (int i=0; i<LEN; i++)  
        a[i] = b[i] + c[i];  
}
```



Aliasing

- Two solutions can be used to avoid the run-time checks
 1. static and global arrays
 2. `__restrict__` attribute



Aliasing

1. Static and Global arrays

```
__attribute__((aligned(16))) float a[LEN];  
__attribute__((aligned(16))) float b[LEN];  
__attribute__((aligned(16))) float c[LEN];
```

```
void func1(){  
    for (int i=0; i<LEN; i++)  
        a[i] = b[i] + c[i];  
}
```

```
int main() {  
    ...  
    func1();  
}
```



Aliasing

1. __restrict__ keyword

```
void func1(float* __restrict__ a, float* __restrict__ b,  
float* __restrict__ c) {  
    __assume_aligned(a, 16);  
    __assume_aligned(b, 16);  
    __assume_aligned(c, 16);  
    for int (i=0; i<LEN; i++)  
        a[i] = b[i] + c[i];  
}  
int main() {  
    float* a=(float*) memalign(16,LEN*sizeof(float));  
    float* b=(float*) memalign(16,LEN*sizeof(float));  
    float* c=(float*) memalign(16,LEN*sizeof(float));  
    ...  
    func1(a,b,c);  
}
```



Aliasing – Multidimensional arrays

- Example with 2D arrays: pointer-to-pointer declaration.

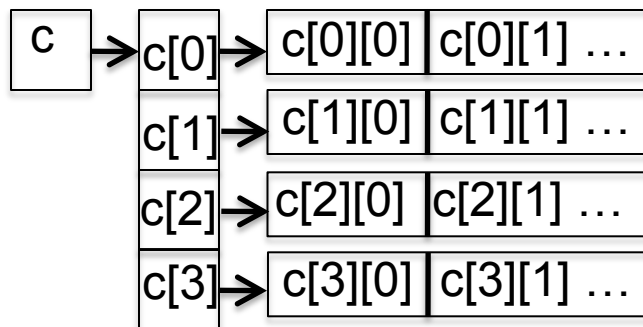
```
void func1(float** __restrict__ a, float**  
__restrict__ b, float** __restrict__ c) {  
    for (int i=0; i<LEN; i++)  
        for (int j=1; j<LEN; j++)  
            a[i][j] = b[i][j-1] * c[i][j];  
}
```



Aliasing – Multidimensional arrays

- Example with 2D arrays: pointer-to-pointer declaration.

```
void func1(float** __restrict__ a, float** __restrict__  
b, float** __restrict__ c) {  
    for (int i=0; i<LEN; i++)  
        for (int j=1; j<LEN; j++)  
            a[i][j] = b[i][j-1] * c[i][j];  
}
```



`__restrict__` only qualifies
the first dereferencing of `c`;

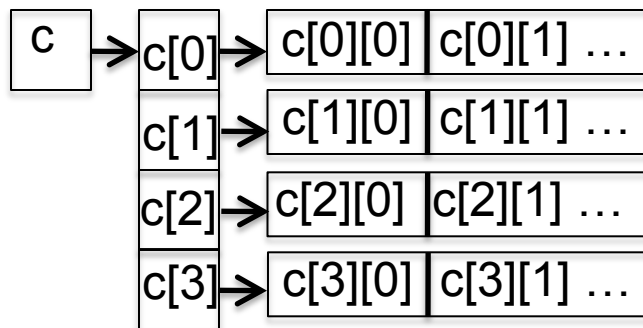
Nothing is said about the
arrays that can be accessed
through `c[i]`



Aliasing – Multidimensional arrays

- Example with 2D arrays: pointer-to-pointer declaration.

```
void func1(float** __restrict__ a, float** __restrict__  
b, float** __restrict__ c) {  
    for (int i=0; i<LEN; i++)  
        for (int j=1; j<LEN; j++)  
            a[i][j] = b[i][j-1] * c[i][j];  
}
```



`__restrict__` only qualifies
the first dereferencing of `c`;

Nothing is said about the
arrays that can be accessed
through `c[i]`

Intel ICC compiler, version 11.1 will vectorize this code.

Previous versions of the Intel compiler or compilers from
other vendors, such as IBM XLC, will not vectorize it.



Aliasing – Multidimensional Arrays

- Three solutions when `__restrict__` does not enable vectorization
 1. Static and global arrays
 2. Linearize the arrays and use `__restrict__` keyword
 3. Use compiler directives



Aliasing – Multidimensional arrays

1. Static and Global declaration

```
__attribute__((aligned(16))) float a[N][N];  
void t(){  
    a[i][j]...  
}  
  
int main() {  
    ...  
    t();  
}
```



Aliasing – Multidimensional arrays

2. Linearize the arrays

```
void t(float* __restrict__ A){
    //Access to Element A[i][j] is now A[i*128+j]
    ...
}

int main() {
    float* A = (float*) memalign(16,128*128*sizeof(float));
    ...
    t(A);
}
```



Aliasing – Multidimensional arrays

3. Use compiler directives:

```
#pragma ivdep (Intel ICC)  
#pragma disjoint(IBM XLC)
```

```
void func1(float **a, float **b, float **c) {  
    for (int i=0; i<m; i++) {  
        #pragma ivdep  
        for (int j=0; j<LEN; j++)  
            c[i][j] = b[i][j] * a[i][j];  
    }  
}
```



Outline

1. Intro
2. Data Dependences (Definition)
3. Overcoming limitations to SIMD-Vectorization
 - Data Dependences
 - Data Alignment
 - Aliasing
 - **Non-unit strides**
 - Conditional Statements
4. Vectorization with intrinsics

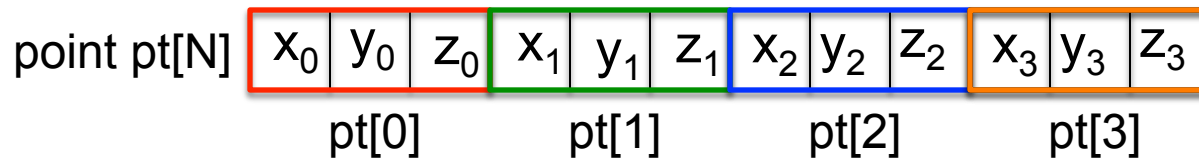


Non-unit Stride – Example I

- Array of a struct

```
typedef struct{int x, y, z}  
point;  
point pt[LEN];
```

```
for (int i=0; i<LEN; i++) {  
    pt[i].y *= scale;  
}
```

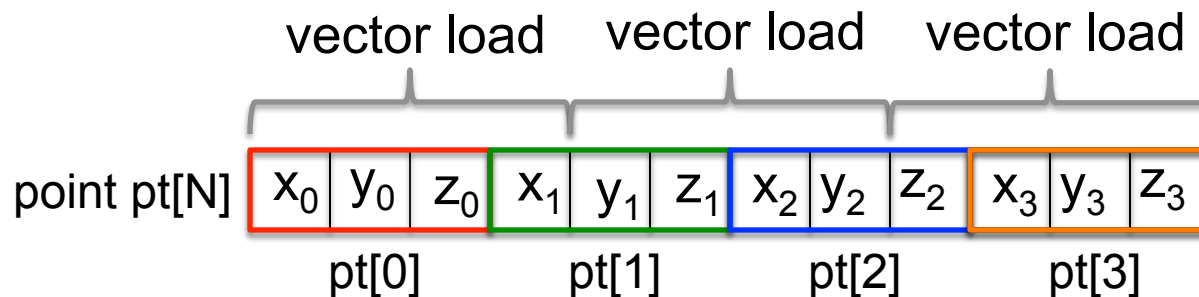


Non-unit Stride – Example I

- Array of a struct

```
typedef struct{int x, y, z}  
point;  
point pt[LEN];
```

```
for (int i=0; i<LEN; i++) {  
    pt[i].y *= scale;  
}
```

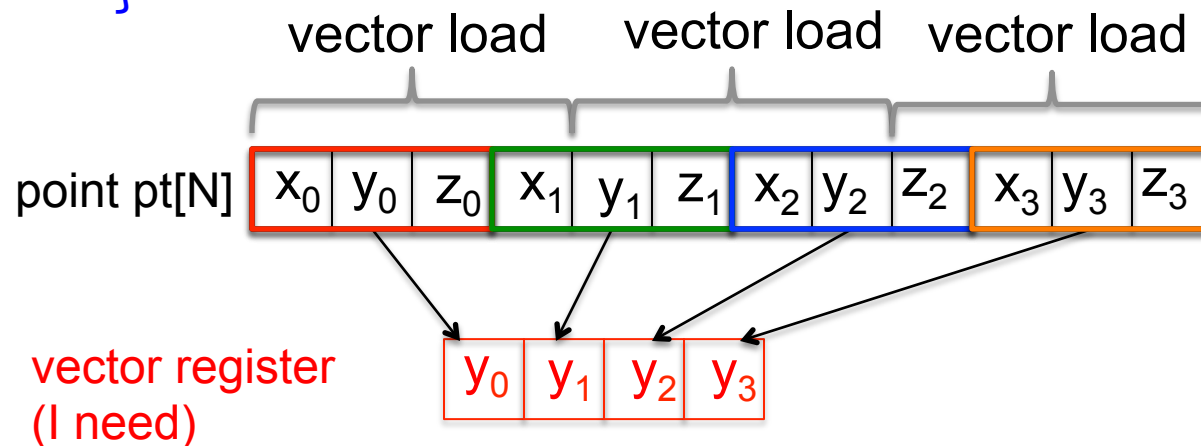


Non-unit Stride – Example I

- Array of a struct

```
typedef struct {int x, y, z}  
point;  
point pt[LEN];
```

```
for (int i=0; i<LEN; i++) {  
    pt[i].y *= scale;  
}
```

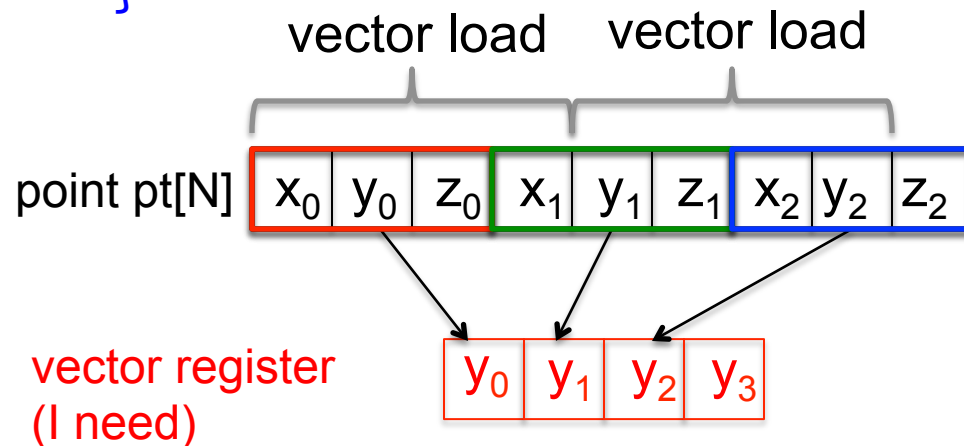


Non-unit Stride – Example I

- Array of a struct

```
typedef struct {int x, y, z;}  
point;  
point pt[LEN];
```

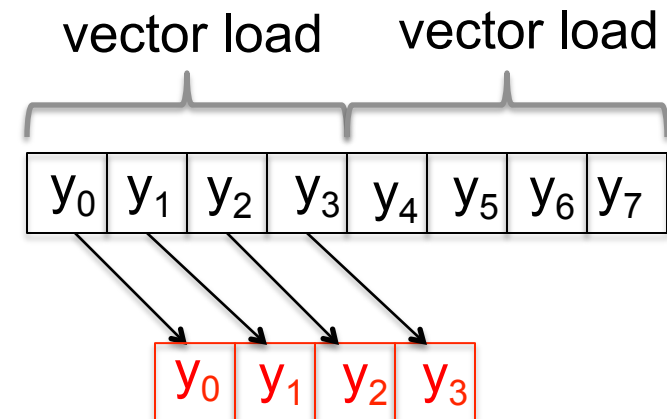
```
for (int i=0; i<LEN; i++) {  
    pt[i].y *= scale;  
}
```



- Arrays

```
int ptx[LEN], int pty[LEN],  
int ptz[LEN];
```

```
for (int i=0; i<LEN; i++) {  
    pty[i] *= scale;  
}
```



Non-unit Stride – Example I

S135

```
typedef struct{int x, y, z}  
point;  
point pt[LEN];  
  
for (int i=0; i<LEN; i++) {  
    pt[i].y *= scale;  
}
```

S135

Intel Nehalem

Compiler report: Loop was not vectorized. Vectorization possible but seems inefficient

Exec. Time scalar code: 6.8

Exec. Time vector code: --

Speedup: --

S135_1

```
int ptx[LEN], int pty[LEN],  
int ptz[LEN];  
  
for (int i=0; i<LEN; i++) {  
    pty[i] *= scale;  
}
```

S135_1

Intel Nehalem

Compiler report: Loop was vectorized.

Exec. Time scalar code: 4.8

Exec. Time vector code: 1.3

Speedup: 3.7



Non-unit Stride – Example I

S135

```
typedef struct{int x, y, z}
point;
point pt[LEN];

for (int i=0; i<LEN; i++) {
    pt[i].y *= scale;
}
```

S135

IBM Power 7

Compiler report: Loop was not SIMD vectorized because it is not profitable to vectorize

Exec. Time scalar code: 2.0

Exec. Time vector code: --

Speedup: --

S135_1

```
int ptx[LEN], int pty[LEN],
int ptz[LEN];

for (int i=0; i<LEN; i++) {
    pty[i] *= scale;
}
```

S135_1

IBM Power 7

Compiler report: Loop was SIMD vectorized

Exec. Time scalar code: 1.8

Exec. Time vector code: 1.5

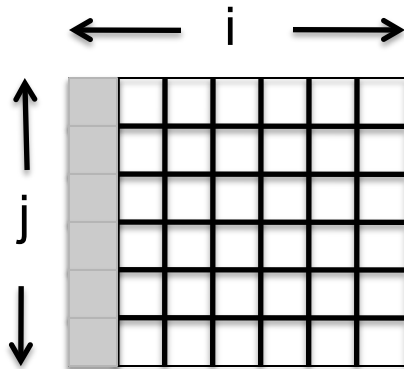
Speedup: 1.2



Non-unit Stride – Example II

```
for (int i=0;i<LEN;i++){  
    sum = 0;  
    for (int j=0;j<LEN;j++){  
        sum += A[j][i];  
    }  
    B[i] = sum;  
}
```

```
for (int i=0;i<size;i++){  
    sum[i] = 0;  
    for (int j=0;j<size;j++){  
        sum[i] += A[j][i];  
    }  
    B[i] = sum[i];  
}
```



Non-unit Stride – Example II

S136

```
for (int i=0;i<LEN;i++){  
    sum = (float) 0.0;  
    for (int j=0;j<LEN;j++){  
        sum += A[j][i];  
    }  
    B[i] = sum;  
}
```

S136_1

```
for (int i=0;i<LEN;i++){  
    sum[i] = (float) 0.0;  
    for (int j=0;j<LEN;j++){  
        sum[i] += A[j][i];  
    }  
    B[i]=sum[i];  
}
```

S136_2

```
for (int i=0;i<LEN;i++){  
    B[i] = (float) 0.0;  
    for (int j=0;j<LEN;j++){  
        B[i] += A[j][i];  
    }  
}
```

S136

Intel Nehalem
Compiler report: Loop was not vectorized. Vectorization possible but seems inefficient
Exec. Time scalar code: 3.7
Exec. Time vector code: --
Speedup: --

S136_1

Intel Nehalem
report: Permuted loop was vectorized.
scalar code: 1.6
vector code: 0.6
Speedup: 2.6

S136_2

Intel Nehalem
report: Permuted loop was vectorized.
scalar code: 1.6
vector code: 0.6
Speedup: 2.6



Non-unit Stride – Example II

S136

```
for (int i=0;i<LEN;i++){
  sum = (float) 0.0;
  for (int j=0;j<LEN;j++){
    sum += A[j][i];
  }
  B[i] = sum;
}
```

S136_1

```
for (int i=0;i<LEN;i++){
  sum[i] = (float) 0.0;
  for (int j=0;j<LEN;j++){
    sum[i] += A[j][i];
  }
  B[i]=sum[i];
}
```

S136_2

```
for (int i=0;i<LEN;i++){
  B[i] = (float) 0.0;
  for (int j=0;j<LEN;j++){
    B[i] += A[j][i];
  }
}
```

S136

IBM Power 7

Compiler report: Loop was not SIMD vectorized

Exec. Time scalar code: 2.0

Exec. Time vector code: --

Speedup: --

S136_1

IBM Power 7

report: Loop interchanging applied.
Loop was SIMD vectorized

scalar code: 0.4

vector code: 0.2

Speedup: 2.0

S136_2

IBM Power 7

report: Loop interchanging applied.
Loop was SIMD

scalar code: 0.4

vector code: 0.16

Speedup: 2.7



Outline

1. Intro
2. Data Dependences (Definition)
3. Overcoming limitations to SIMD-Vectorization
 - Data Dependences
 - Data Alignment
 - Aliasing
 - Non-unit strides
 - **Conditional Statements**
4. Vectorization with intrinsics



Conditional Statements – I

- Loops with conditions need `#pragma vector always`
 - Since the compiler does not know if vectorization will be profitable
 - The condition may prevent from an exception

```
#pragma vector always
for (int i = 0; i < LEN; i++){
    if (c[i] < (float) 0.0)
        a[i] = a[i] * b[i] + d[i];
}
```



Conditional Statements – I

S137

```
for (int i = 0; i < LEN; i++){  
    if (c[i] < (float) 0.0)  
        a[i] = a[i] * b[i] + d[i];  
}
```

S137_1

```
#pragma vector always  
for (int i = 0; i < LEN; i++){  
    if (c[i] < (float) 0.0)  
        a[i] = a[i] * b[i] + d[i];  
}
```

S137

Intel Nehalem

Compiler report: Loop was not vectorized. Condition may protect exception

Exec. Time scalar code: 10.4

Exec. Time vector code: --

Speedup: --

S137_1

Intel Nehalem

Compiler report: Loop was vectorized.

Exec. Time scalar code: 10.4

Exec. Time vector code: 5.0

Speedup: 2.0



Conditional Statements – I

S137

```
for (int i = 0; i < LEN; i++){  
    if (c[i] < (float) 0.0)  
        a[i] = a[i] * b[i] + d[i];  
}
```

S137_1

```
for (int i = 0; i < LEN; i++){  
    if (c[i] < (float) 0.0)  
        a[i] = a[i] * b[i] + d[i];  
}
```

compiled with flag -qdebug=alwayspec

S137

IBM Power 7

Compiler report: Loop was SIMD
vectorized

Exec. Time scalar code: 4.0

Exec. Time vector code: 1.5

Speedup: 2.5

S137_1

IBM Power 7

Compiler report: Loop was SIMD
vectorized

Exec. Time scalar code: 4.0

Exec. Time vector code: 1.5

Speedup: 2.5



Conditional Statements

- Compiler removes *if conditions* when generating vector code

```
for (int i = 0; i < LEN; i++){  
    if (c[i] < (float) 0.0)  
        a[i] = a[i] * b[i] + d[i];  
}
```



Conditional Statements

```
for (int i=0;i<1024;i++){
    if (c[i] < (float) 0.0)
        a[i]=a[i]*b[i]+d[i];
}
```

rC	2	-1	1	-2
rCmp	False	True	False	True
rThen	0	3.2	0	3.2
rElse	1.	0	1.	0
rS	1.	3.2	1.	3.2

```
vector bool char = rCmp
vector float r0={0.,0.,0.,0.};
vector float rA,rB,rC,rD,rS, rT,
rThen,rElse;
for (int i=0;i<1024;i+=4){
    // load rA, rB, and rD;
    rCmp = vec_cmplt(rC, r0);
    rT= rA*rB+rD;
    rThen = vec_and(rT.rCmp);
    rElse = vec_andc(rA.rCmp);
    rS = vec_or(rthen, relse);
    //store rS
}
```



Conditional Statements

```
for (int i=0;i<1024;i++){  
    if (c[i] < (float) 0.0)  
        a[i]=a[i]*b[i]+d[i];  
}
```

Speedups will depend on the values on c[i]

Compiler tends to be conservative, as the condition may prevent from segmentation faults

```
vector bool char = rCmp  
vector float r0={0.,0.,0.,0.};  
vector float rA,rB,rC,rD,rS, rT,  
rThen,rElse;  
for (int i=0;i<1024;i+=4){  
    // load rA, rB, and rD;  
    rCmp = vec_cmplt(rC, r0);  
    rT= rA*rB+rD;  
    rThen = vec_and(rT.rCmp);  
    rElse = vec_andc(rA.rCmp);  
    rS = vec_or(rthen, relse);  
    //store rS  
}
```



Compiler Directives

- Compiler vectorizes many loops, but many more can be vectorized if the appropriate directives are used

Compiler Hints for Intel ICC	Semantics
<code>#pragma ivdep</code>	Ignore assume data dependences
<code>#pragma vector always</code>	override efficiency heuristics
<code>#pragma novector</code>	disable vectorization
<code>__restrict__</code>	assert exclusive access through pointer
<code>__attribute__((aligned(int-val)))</code>	request memory alignment
<code>memalign(int-val,size);</code>	malloc aligned memory
<code>__assume_aligned(exp, int-val)</code>	assert alignment property



Compiler Directives

- Compiler vectorizes many loops, but many more can be vectorized if the appropriate directives are used

Compiler Hints for IBM XLC	Semantics
<code>#pragma ibm independent_loop</code>	Ignore assumed data dependences
<code>#pragma nosimd</code>	disable vectorization
<code>__restrict__</code>	assert exclusive access through pointer
<code>__attribute__((aligned(int-val)))</code>	request memory alignment
<code>memalign(int-val,size);</code>	malloc aligned memory
<code>__alignx (int-val, exp)</code>	assert alignment property



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4. Vectorization with intrinsics



Access the SIMD through intrinsics

- Intrinsics are vendor/architecture specific
- We will focus on the Intel vector intrinsics
- Intrinsics are useful when
 - the compiler fails to vectorize
 - when the programmer thinks it is possible to generate better code than the one produced by the compiler



The Intel SSE intrinsics Header file

- SSE can be accessed using intrinsics.
- You must use one of the following header files:
 - `#include <xmmintrin.h>` (for SSE)
 - `#include <emmintrin.h>` (for SSE2)
 - `#include <pmmmintrin.h>` (for SSE3)
 - `#include <smmintrin.h>` (for SSE4)
- These include the prototypes of the intrinsics.



Intel SSE intrinsics Data types

- We will use the following data types:
 - `__m128` packed single precision (vector XMM register)
 - `__m128d` packed double precision (vector XMM register)
 - `__m128i` packed integer (vector XMM register)
- Example

```
#include <xmmintrin.h>
int main ( ) {
    ...
    __m128 A, B, C; /* three packed s.p. variables */
    ...
}
```



Intel SSE intrinsic Instructions

- Intrinsics operate on these types and have the format:

`_mm_instruction_suffix(...)`

- Suffix can take many forms. Among them:

`ss` scalar single precision

`ps` packed (vector) single precision

`sd` scalar double precision

`pd` packed double precision

`si#` scalar integer (8, 16, 32, 64, 128 bits)

`su#` scalar unsigned integer (8, 16, 32, 64, 128 bits)



Intel SSE intrinsics

Instructions – Examples

- Load four 16-byte aligned single precision values in a vector:

```
float a[4]={1.0,2.0,3.0,4.0}; //a must be 16-byte aligned  
__m128 x = _mm_load_ps(a);
```

- Add two vectors containing four single precision values:

```
__m128 a, b;  
__m128 c = _mm_add_ps(a, b);
```



Intrinsics (SSE)

```
#define n 1024
__attribute__((aligned(16)))
float a[n], b[n], c[n];
```

```
int main() {
    for (i = 0; i < n; i++) {
        c[i]=a[i]*b[i];
    }
}
```

```
#include <xmmintrin.h>
#define n 1024
__attribute__((aligned(16))) float
a[n], b[n], c[n];
```

```
int main() {
    __m128 rA, rB, rC;
    for (i = 0; i < n; i+=4) {
        rA = _mm_load_ps(&a[i]);
        rB = _mm_load_ps(&b[i]);
        rC= _mm_mul_ps(rA,rB);
        _mm_store_ps(&c[i], rC);
    }
}
```



Intel SSE intrinsics

A complete example

```
#define n 1024
```

```
int main() {  
    float a[n], b[n], c[n];  
    for (i = 0; i < n; i+=4) {  
        c[i:i+3]=a[i:i+3]+b[i:i+3];  
    }  
}
```

Header file

```
#include <xmmintrin.h>
```

```
#define n 1024
```

```
__attribute__((aligned(16))) float  
a[n], b[n], c[n];
```

```
int main() {  
    __m128 rA, rB, rC;  
    for (i = 0; i < n; i+=4) {  
        rA = _mm_load_ps(&a[i]);  
        rB = _mm_load_ps(&b[i]);  
        rC = _mm_mul_ps(rA, rB);  
        _mm_store_ps(&c[i], rC);  
    }  
}
```



Intel SSE intrinsics

A complete example

```
#define n 1024
```

```
int main() {  
    float a[n], b[n], c[n];  
    for (i = 0; i < n; i+=4) {  
        c[i:i+3]=a[i:i+3]  
    }  
}
```

Declare 3 vector registers



```
#include <xmmintrin.h>
```

```
#define n 1024
```

```
__attribute__((aligned(16))) float  
a[n], b[n], c[n];
```

```
int main() {  
    __m128 rA, rB, rC;  
    for (i = 0; i < n; i+=4) {  
        rA = _mm_load_ps(&a[i]);  
        rB = _mm_load_ps(&b[i]);  
        rC = _mm_mul_ps(rA, rB);  
        _mm_store_ps(&c[i], rC);  
    }  
}
```



Intel SSE intrinsics

A complete example

```
#define n 1000
```

```
int main() {  
    float a[n], b[n], c[n];  
    for (i = 0; i < n; i+=4) {  
        c[i:i+3]=a[i:i+3]+b[i:i+3];  
    }  
}
```



Execute vector
statements

```
#include <xmmintrin.h>
```

```
#define n 1024
```

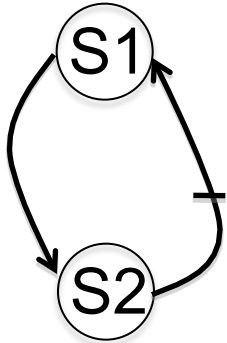
```
__attribute__((aligned(16))) float  
a[n], b[n], c[n];
```

```
int main() {  
    __m128 rA, rB, rC;  
    for (i = 0; i < n; i+=4) {  
        rA = _mm_load_ps(&a[i]);  
        rB = _mm_load_ps(&b[i]);  
        rC = _mm_mul_ps(rA, rB);  
        _mm_store_ps(&c[i], rC);  
    }  
}
```

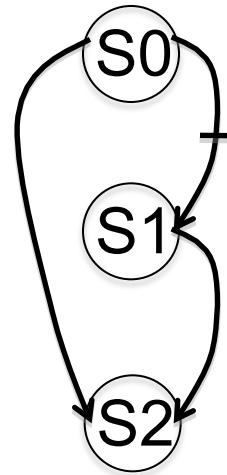


Node Splitting

```
for (int i=0;i<LEN-1;i++){  
S1  a[i]=b[i]+c[i];  
S2  d[i]=(a[i]+a[i+1])*(float)0.5;  
}
```



```
for (int i=0;i<LEN-1;i++){  
S0 temp[i]=a[i+1];  
S1 a[i]=b[i]+c[i];  
S2 d[i]=(a[i]+temp[i])*(float) 0.5;  
}
```



Node Splitting with intrinsics

```
for (int i=0;i<LEN-1;i++){
    a[i]=b[i]+c[i];
    d[i]=(a[i]+a[i+1])*(float)0.5;
}
```

```
for (int i=0;i<LEN-1;i++){
    temp[i]=a[i+1];
    a[i]=b[i]+c[i];
    d[i]=(a[i]+temp[i])*(float)0.5;
}
```

Which code runs faster ?

Why?

```
#include <xmmintrin.h>
#define n 1000

int main() {
    __m128 rA1, rA2, rB, rC, rD;
    __m128 r5=_mm_set1_ps((float)0.5)
    for (i = 0; i < LEN-4; i+=4) {
        rA2= _mm_loadu_ps(&a[i+1]);
        rB= _mm_load_ps(&b[i]);
        rC= _mm_load_ps(&c[i]);
        rA1= _mm_add_ps(rB, rC);
        rD= _mm_mul_ps(_mm_add_ps(rA1,rA2),r5);
        _mm_store_ps(&a[i], rA1);
        _mm_store_ps(&d[i], rD);
    }
}
```



Node Splitting with intrinsics

S126

```
for (int i=0;i<LEN-1;i++){  
    a[i]=b[i]+c[i];  
    d[i]=(a[i]+a[i+1])*(float)0.5;  
}
```

S126_1

```
for (int i=0;i<LEN-1;i++){  
    temp[i]=a[i+1];  
    a[i]=b[i]+c[i];  
    d[i]=(a[i]+temp[i])*(float)0.5;  
}
```

S126_2

```
#include <xmmintrin.h>  
#define n 1000  
  
int main() {  
    __m128 rA1, rA2, rB, rC, rD;  
    __m128 r5=_mm_set1_ps((float)0.5)  
    for (i = 0; i < LEN-4; i+=4) {  
        rA2= _mm_loadu_ps(&a[i+1]);  
        rB= _mm_load_ps(&b[i]);  
        rC= _mm_load_ps(&c[i]);  
        rA1= _mm_add_ps(rB, rC);  
        rD= _mm_mul_ps(_mm_add_ps(rA1, rA2), r5);  
        _mm_store_ps(&a[i], rA1);  
        _mm_store_ps(&d[i], rD);  
    }  
}
```



Node Splitting with intrinsics

S126

Intel Nehalem

Compiler report: Loop was not vectorized. Existence of vector dependence

Exec. Time scalar code: 12.6

Exec. Time vector code: --

Speedup: --

S126_1

Intel Nehalem

Compiler report: Loop was vectorized.

Exec. Time scalar code: 13.2

Exec. Time vector code: 9.7

Speedup: 1.3

S126_2

Intel Nehalem

Exec. Time intrinsics: 6.1

Speedup (versus vector code): 1.6



Node Splitting with intrinsics

S126

IBM Power 7

Compiler report: Loop was SIMD vectorized

Exec. Time scalar code: 3.8

Exec. Time vector code: 1.7

Speedup: 2.2

S126_1

IBM Power 7

Compiler report: Loop was SIMD vectorized

Exec. Time scalar code: 5.1

Exec. Time vector code: 2.4

Speedup: 2.0

S126_2

IBM Power 7

Exec. Time intrinsics: 1.6

Speedup (versus vector code): 1.5



Summary

- Microprocessor vector extensions can contribute to improve program performance and the amount of this contribution is likely to increase in the future as vector lengths grow.
- Compilers are only partially successful at vectorizing
- When the compiler fails, programmers can
 - add compiler directives
 - apply loop transformations
- If after transforming the code, the compiler still fails to vectorize (or the performance of the generated code is poor), the only option is to program the vector extensions directly using intrinsics or assembly language.



Data Dependences

- The correctness of many many loop transformations including vectorization can be decided using dependences.
- A good introduction to the notion of dependence and its applications can be found in D. Kuck, R. Kuhn, D. Padua, B. Leasure, M. Wolfe: Dependence Graphs and Compiler Optimizations. POPL 1981.



Compiler Optimizations

- For a longer discussion see:
 - Kennedy, K. and Allen, J. R. 2002 Optimizing Compilers for Modern Architectures: a Dependence-Based Approach. Morgan Kaufmann Publishers Inc.
 - U. Banerjee. Dependence Analysis for Supercomputing. Kluwer Academic Publishers, Norwell, Mass., 1988.
 - Advanced Compiler Optimizations for Supercomputers, by David Padua and Michael Wolfe in Communications of the ACM, December 1986, Volume 29, Number 12.
 - Compiler Transformations for High-Performance Computing, by David Bacon, Susan Graham and Oliver Sharp, in ACM Computing Surveys, Vol. 26, No. 4, December 1994.



Algorithms

- W. Daniel Hillis and Guy L. Steele, Jr.. 1986.
Data parallel algorithms. *Commun. ACM* 29, 12
(December 1986), 1170-1183.
- Shyh-Ching Chen, D.J. Kuck, "Time and Parallel
Processor Bounds for Linear Recurrence
Systems," *IEEE Transactions on Computers*, pp.
701-717, July, 1975



Thank you

Questions?

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Program Optimization Through Loop Vectorization

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Back-up Slides



Measuring execution time

```
time1 = time();  
  
for (i=0; i<32000; i++)  
    c[i] = a[i] + b[i];  
  
time2 = time();
```



Measuring execution time

- Added an outer loop that runs (serially)
 - to increase the running time of the loop

```
time1 = time();  
for (j=0; j<200000; j++){  
    for (i=0; i<32000; i++)  
        c[i] = a[i] + b[i];  
}  
time2 = time();
```



Measuring execution times

- Added an outer loop that runs (serially)
 - to increase the running time of the loop
- **Call a dummy () function that is compiled separately**
 - to avoid loop interchange or dead code elimination

```
time1 = time();  
for (j=0; j<200000; j++){  
    for (i=0; i<32000; i++)  
        c[i] = a[i] + b[i];  
    dummy();  
}  
time2 = time();
```



Measuring execution times

- Added an outer loop that runs (serially)
 - to increase the running time of the loop
- Call a dummy () function that is compiled separately
 - to avoid loop interchange or dead code elimination
- **Access the elements of one output array and print the result**
 - to avoid dead code elimination

```
time1 = time();
for (j=0; j<200000; j++){
    for (i=0; i<32000; i++)
        c[i] = a[i] + b[i];
    dummy();
}
time2 = time();
for (j=0; j<32000; j++)
    ret+= a[j];
printf ("Time %f, result %f", (time2 -time1), ret);
```



Compiling

- Intel icc scalar code

icc -O3 –no-vec dummy.o tsc.o –o runnovec

- Intel icc vector code

icc -O3 –vec-report[n] –xSSE4.2 dummy.o tsc.o –o runvec

[n] can be 0,1,2,3,4,5

- **vec-report0**, no report is generated
- **vec-report1**, indicates the line number of the loops that were vectorized
- **vec-report2 .. 5**, gives a more detailed report that includes the loops that were not vectorized and the reason for that.



Compiling

```
flags = -O3 -qaltivec -qhot -qarch=pwr7 -qtune=pwr7  
-qipa=malloc16 -qdebug=NSIMDCOST  
-qdebug=alwayspec -qreport
```

- IBM xlc scalar code
xlc -qnoenablevmx dummy.o tsc.o -o runnovec
- IBM vector code
xlc -qenablevmx dummy.o tsc.o -o runvec



Strip Mining

This transformation improves locality and is usually combined with vectorization



Strip Mining

```
for (i=1; i<LEN; i++) {  
    a[i]= b[i];  
    c[i] = c[i-1] + a[i];  
}
```

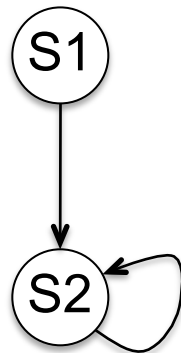


```
for (i=1; i<LEN; i++)  
    a[i]= b[i];  
  
for (i=1; i<LEN; i++)  
    c[i] = c[i-1] + a[i];
```

- first statement can be vectorized
- second statement cannot be vectorized because of self-true dependence

By applying loop distribution the compiler will vectorize the first statement

But, ... loop distribution will increase the cache miss ratio if array a[] is large



Strip Mining

Loop Distribution

```
for (i=1; i<LEN; i++)  
    a[i]= b[i];  
for (i=1; i<LEN; i++)  
    c[i] = c[i-1] + a[i];
```



Strip Mining

```
for (i=1; i<LEN; i  
+=strip_size){  
    for (j=i; j<strip_size; j++)  
        a[j]= b[j];  
    for (j=i; j<strip_size; j++)  
        c[j] = c[j-1] + a[j];  
}
```

strip_size is usually a small value (4, 8, 16 or 32).



Strip Mining

- Another example

```
int v[N];  
...  
for (int i=0;i<N;i++){  
    Transform (v[i]);  
}  
for (int i=0;i<N;i++){  
    Light (v[i]);  
}
```

```
int v[N];  
...  
for (int i=0;i<N;i+=strip_size){  
    for (int j=i;j<strip_size;j++){  
        Transform (v[j]);  
    }  
    for (int j=i;j<strip_size;j++){  
        Light (v[j]);  
    }  
}
```

